

① Find f_x , f_y , f_{xy} , f_{xx} , f_{yy} for $f(x,y) = \sin^2(x-3y)$.
(#17 on 14.3)

② Find $\frac{\partial w}{\partial r}$ if $w = (x+y+z)^2$ $x=r-s$ $y=\cos(r+s)$
(#33 on 14.4) $z=s\ln(r+s)$

③ Find directional derivative $f(x,y) = \frac{x-y}{xy+2}$ $\vec{u} = 12\hat{i} + 5\hat{j}$
(#13 on 14.5) at $P_0(1, -1)$

④ Find the directions that f increase most rapidly
decrease most rapidly
(#20 on 14.5) $f(x,y) = x^2y + e^{xy}\sin y$ at $P_0(1,0)$

⑤ Find tangent plane and normal line of
(#4. on 14.6) $x^2 + 2xy - y^2 + z^2 = 7$ at $P_0(1, -1, 3)$

⑥ Find tangent line of the intersection line between
the two surfaces $xyz=1$
(#14 on 14.6) $x^2 + 2y^2 + 3z^2 = 6$ at pt $(1, 1, 1)$.

⑦ Find absolute extreme values of
(#34 on 14.7) $T(x,y) = x^2 + xy + y^2 - 6x$ on $0 \leq x \leq 5$ $-3 \leq y \leq 3$.

⑧ Find $\int_1^4 \int_0^4 \left(\frac{x}{z} + \sqrt{y}\right) dx dy$.

(#57 on 15.2) $\iint_R \frac{\sqrt{x}}{y^2} dA$ $R: 0 \leq x \leq 4$ $1 \leq y \leq 2$

⑨ Find volume of $z = x^2 + y^2$ and below by $\begin{cases} y=x \\ x+y=2 \end{cases}$

⑩ Find Area bounded by ~~$y=x$~~ $y=-x$, $x=y^2$ and $x=2y^2 - 2$.
(#8 on 15.3)