

A collection of objects is said to form a **sequence** if the collection is ordered so that it has a first member, a second member, a third member, and so on. Below are two examples of sequences of numbers, the numbers in the sequences are called **terms**.

SEQUENCE 1:

3, 6, 9, 12, 15

SEQUENCE 2:

3, 6, 9, 12, 15, . . .

You can think of a sequence as a function whose domain is a set of consecutive integers. If a domain is not specified, it is understood that the domain starts with 1.

DOMAIN:    1   2   3   4   5    The domain gives the relative position of each term: 1st, 2nd, 3rd, and so on.  
 RANGE:    3   6   9   12   15                      The range gives the terms of the sequence.

Sequence 1 is a **finite sequence** because it has a last term. Sequence 2 is an **infinite sequence** because it continues without stopping. Both sequences have the general rule  $a_n = 3n$  where  $a_n$  represents the  $n^{\text{th}}$  term of the sequence,  $\{a_n\}_1^\infty$ . The general rule can also be written using function notation:  $f(n) = 3n$ .

1. Write the first 4 terms of the sequence with general terms:

- $a_n = 3n + 1$

- $\{(-2)^{n+1}\}$

2. For each sequence, write a rule for the  $n^{\text{th}}$  term

- $-\frac{1}{3}, \frac{1}{9}, -\frac{1}{27}, \frac{1}{81}, \dots$

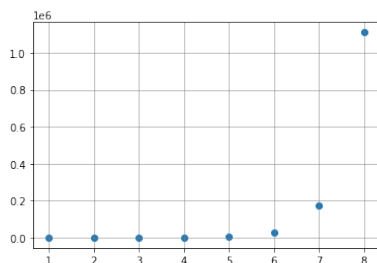
- 2, 6, 12, 20, . . .

If  $\{a_n\}$  is a sequence, and if  $f(x)$  is a continuous function with  $f(n) = a_n$  for all  $n > N$  for some number  $N$  then

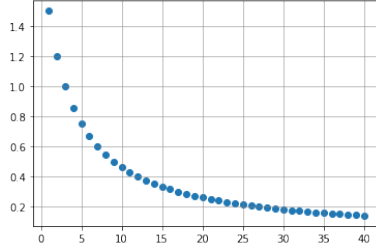
$$\lim_{n \rightarrow \infty} a_n = \lim_{x \rightarrow \infty} f(x)$$

3. Determine if each sequence converges or diverges

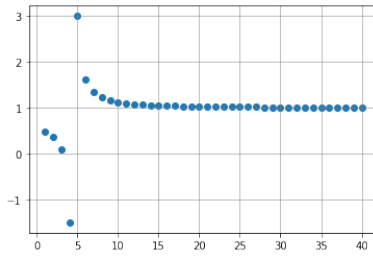
- $a_n = \frac{e^{2n}}{n}$



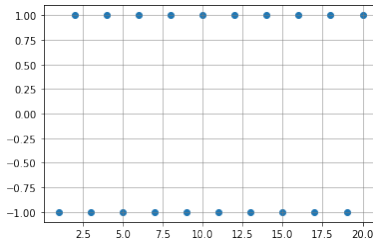
- $a_n = \frac{6}{n+3}$



- $a_n = \frac{n^2 - 10}{n^2 - 20}$



- $\{(-1)^n\}$



- $\left\{ \frac{(-1)^n}{n} \right\}$

