

§4.3 #1 $X =$ waiting time until $\alpha = 10^{\text{th}}$ change with $\theta = \frac{1}{(7/3)} = \frac{3}{2}$.

so

(a) pdf of X is a gamma distribution: $\alpha = 10, \theta = 3/2$.

$$f(x) = \frac{1}{\Gamma(10)(3/2)^{10}} x^9 e^{-2x/3}, \quad 0 \leq x$$

(b) From bottom of page 187 of text, where we derived

$$\mu = \alpha\theta = 15, \quad \sigma^2 = \alpha\theta^2 = 45/2$$

#9 (a) X is $\chi^2(17)$, then $r = 17 \Rightarrow$

$$P(X < 7.564) = .024997$$

$$(c) P(6.408 < X < 27.59) = .940035$$

§4.4**#1** Z is standard normal

$$(a) P(.53 < Z \leq 2.06) = \Phi(2.06) - \Phi(.53) = .2784$$

$$(b) P(-.79 < Z < 1.52) = \Phi(1.52) - \Phi(-.79) = \Phi(1.52) + \Phi(.79) - 1$$

$\xleftarrow{\text{symmetry}} = .72098 \xleftarrow{\text{symmetry}}$

$$(c) P(Z > -1.77) = P(Z < +1.77) = .96164$$

$$(d) P(Z > 2.89) = 1 - P(Z < 2.89) = .001926$$

$$(f) P(|Z| < 1) = P(-1 < Z < 1) = 2\Phi(1) - 1 = .682689$$

$\xleftarrow{\text{symmetry}}$