

Homework 9 additional problems.

1. Let  $F(x) = x \sin(1/x)$  for  $x \neq 0$  and  $F(0) = 0$ . Find  $\overline{D^+}F(0)$ ,  $\overline{D^-}F(0)$ ,  $\underline{D^+}F(0)$ , and  $\underline{D^-}F(0)$ .
2. Let  $F : [a, b] \rightarrow \mathbb{R}$  be a continuous function and assume  $F$  has a local minimum at  $c \in (a, b)$ . Prove that

$$\overline{D^-}F(c) \leq 0 \leq \underline{D^+}F(c).$$