

MATH 544  
Spring, 2009

Quiz #2

Name: \_\_\_\_\_

1. For which value(s) of  $h$  will  $\mathbf{y} = \begin{bmatrix} -4 \\ 3 \\ h \end{bmatrix}$  be in  $\text{span}(\{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\})$  if

$$\mathbf{v}_1 = \begin{bmatrix} 1 \\ -1 \\ -2 \end{bmatrix}, \quad \mathbf{v}_2 = \begin{bmatrix} 5 \\ -4 \\ -7 \end{bmatrix}, \quad \text{and} \quad \mathbf{v}_3 = \begin{bmatrix} -3 \\ 1 \\ 0 \end{bmatrix}?$$

Assuming that  $h$  has an appropriate value, express  $\mathbf{y}$  as a linear combination of  $\mathbf{v}_1$ ,  $\mathbf{v}_2$ , and  $\mathbf{v}_3$ .

2. In the problem above, can  $\mathbf{y}$  be expressed in more than one way as a linear combination of  $\mathbf{v}_1$ ,  $\mathbf{v}_2$ , and  $\mathbf{v}_3$ . If so, do it; if not, explain why not.
3. (Bonus) What do the previous results tell us about the independence or dependence of the set  $\{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\}$ ?