

(a) $\lim_{x \rightarrow \infty} \arctan(7x) = \frac{\pi}{2}$, so $\lim_{x \rightarrow \infty} e^{\arctan(7x)} = e^{\pi/2} [\approx 4.81]$, so $y = e^{\pi/2}$ is a HA. $\lim_{x \rightarrow -\infty} e^{\arctan(7x)} = e^{-\pi/2} [\approx 0.21]$, so $y = e^{-\pi/2}$ is a HA.

(b) $f(x) = e^{\arctan(7x)} \Rightarrow f'(x) = e^{\arctan(7x)} \cdot \frac{7}{1+49x^2} > 0$ for all x . Thus, f is increasing on \mathbb{R} .

$$\begin{aligned} \text{(c) } f''(x) &= e^{\arctan(7x)} \left[\frac{-686x}{(1+49x^2)^2} \right] + \frac{7}{1+49x^2} \cdot e^{\arctan(7x)} \cdot \frac{7}{1+49x^2} \\ &= \frac{7e^{\arctan(7x)}}{(1+49x^2)^2} (-98x+7) \end{aligned}$$

$f''(x) > 0 \Leftrightarrow -98x+7 > 0 \Leftrightarrow x < 0.07$ and $f''(x) < 0 \Leftrightarrow x > 0.07$, so f is CU on $(-\infty, 0.07)$ and f is CD on $(0.07, \infty)$. There is an inflection point at $(0.07, f(0.07)) = (0.07, e^{\arctan(0.49)}) \approx (0.07, 1.58)$.

(d)

