MATH 141 (Section 3 & 4) Prof. Meade

Exam 1 September 9, 2009 University of South Carolina Fall 2009

Instructions:

- 1. There are a total of 8 problems on 6 pages. Check that your copy of the exam has all of the problems.
- 2. Calculators may not be used for any portion of this exam.
- 3. You must show all of your work to receive credit for a correct answer.
- 4. Your answers must be written legibly in the space provided. You may use the back of a page for additional space; please indicate clearly when you do so.

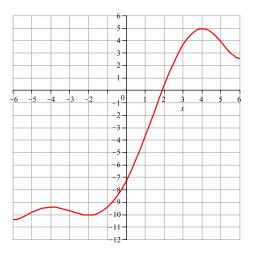
Problem	Points	Score
1	8	
2	10	
3	16	
4	18	
5	12	
6	12	
7	6	
8	18	
Total	100	

- 1. (8 points) Suppose the graph of f is given. Write an equation for each of the graphs that are obtained from the graph of f as follows.
 - (a) shift 3 units upward
 - (b) shift 1 unit downward
 - (c) shift 2 units to the right
 - (d) reflect about the x-axis

- 2. (10 points) Determine whether the statement is true or false. In either case, give a short explanation why.
 - (a) If f is a function, then f(5x) = 5f(x).
 - (b) A horizontal line intersects the graph of a function at most once.
 - (c) You can always divide by e^x .
 - (d) If x > 0, then $\ln(x^6) = 6\ln(x)$.

(e)
$$\tan^{-1}(x) = \frac{\sin^{-1}(x)}{\cos^{-1}(x)}$$
, provided $\cos^{-1}(x) \neq 0$.

3. (16 points) Use the graph of the function f in the figure below to answer the following questions.



- (a) Find f(-2).
- (b) Estimate the value(s) of x such that f(x) = -4.
- (c) On what interval(s) is f decreasing?
- (d) What is the largest interval containing x = 0 on which f is invertible?
- 4. (18 points)
 - (a) Find the exact value of the expression: $\arctan\left(\frac{1}{\sqrt{3}}\right)$.
 - (b) Find the exact value of the expression: $\arcsin\left(\sin\left(\frac{7\pi}{3}\right)\right)$.
 - (c) Simplify the expression: $\sin(2\arctan(x))$.

HINT: Draw, and label, a right triangle. NOTE: Your final answer should be a rational function.

5. (12 points) If $f(x) = x^2 - 2x + 3$, evaluate the difference quotient

$$\frac{f(a+h) - f(a)}{h}.$$

NOTE: Your final answer should not involve a fraction.

6. (12 points) Solve for x: $\ln(x) - \ln(x - 1) = 1$.

7. (6 points) The table shows the position of a cyclist during the first 10 seconds of a ride.

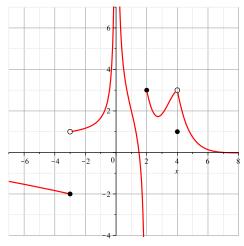
t (seconds)	0	1	2	4	6	10
s (meters)	0	8.2	17.4	35.2	58.3	95.8

Find the average velocity over the given time periods:

(a) [1, 6]

(b) [0, 10]

8. (18 points) The graph of f is shown in the figure. Note that f has vertical asymptotes at x = 0 and x = 2.



Find each number, or explain why it does not exist.

- (a) f(-3)
- (b) $\lim_{x \to -3^-} f(x)$
- (c) $\lim_{x \to -3} f(x)$
- (d) $\lim_{x \to 0} f(x)$
- (e) f(0)
- (f) $\lim_{x \to 2^+} f(x)$
- (g) f(4)
- (h) $\lim_{x \to 4} f(x)$
- (i) $\lim_{x \to \infty} f(x)$