

PRINT Your Name: _____

Quiz for May 30, 2006

Find the general solution of the following system of linear equations:

$$\begin{aligned} x_1 + x_2 - x_5 &= 1 \\ x_2 + 2x_3 + x_4 + 3x_5 &= 1 \\ x_1 - x_3 + x_4 + x_5 &= 0. \end{aligned}$$

Also find **three** particular solutions of this system of equations. **Be sure to check** that all three of your particular solutions really satisfy the original system of linear equations.

$$\left[\begin{array}{ccccc|c} 1 & 1 & 0 & 0 & -1 & 1 \\ 0 & 1 & 2 & 1 & 3 & 1 \\ 1 & 0 & -1 & 1 & 1 & 0 \end{array} \right] \begin{array}{l} R_3 \rightarrow R_3 - R_1 \\ R_3 \rightarrow R_3 + R_2 \\ R_1 \rightarrow R_1 - R_2 \end{array}$$

$$\left[\begin{array}{ccccc|c} 1 & 0 & -2 & -1 & -4 & 0 \\ 0 & 1 & 2 & 1 & 3 & 1 \\ 0 & 0 & 1 & 2 & 5 & 0 \end{array} \right] \begin{array}{l} R_2 \rightarrow R_2 - 2R_3 \\ R_1 \rightarrow R_1 + 2R_3 \end{array}$$

$$\left[\begin{array}{ccccc|c} 1 & 0 & 0 & 3 & 6 & 0 \\ 0 & 1 & 0 & -3 & -7 & 1 \\ 0 & 0 & 1 & 2 & 5 & 0 \end{array} \right]$$

So

$$\begin{aligned} x_1 &= -3x_4 - 6x_5 \\ x_2 &= 1 + 3x_4 + 7x_5 \\ x_3 &= -2x_4 - 5x_5 \\ x_4 &= x_4 \\ x_5 &= x_5 \end{aligned}$$

General solution

3 particular solutions

$$\begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} -3 \\ 4 \\ -2 \\ 1 \\ 0 \end{bmatrix}, \begin{bmatrix} -6 \\ 8 \\ -5 \\ 0 \\ 1 \end{bmatrix}$$

check

$$\begin{array}{l} 1 = 1 \\ 1 = 1 \\ 0 = 0 \end{array} \quad \begin{array}{l} -3 + 4 = 1 \\ 4 - 4 + 1 = 1 \\ -3 + 2 + 1 = 0 \end{array} \quad \begin{array}{l} -6 + 8 - 1 = 1 \\ 8 - 10 + 3 = 1 \\ -6 + 5 + 1 = 0 \end{array}$$