

PRINT Your Name: _____

There are 17 problems on 10 pages. The exam is worth 200 points. SHOW your work. **CIRCLE** your answer. **CHECK** your answer whenever possible. **NO CALCULATORS.**

1. (20 points) Let A be an $n \times n$ matrix. List 8 statements that are equivalent to the statement " A is nonsingular".

- 1) A is nonsingular
- 2) The only vector x with $Ax=0$ is $x=0$
- 3) The null space of $A=0$.
- 4) The dimension of the null space of A is zero.
- 5) The rank of $A=n$
- 6) The dimension of the col. space of A is n
- 7) the cols of A are l.i.
- 8) the cols of A span \mathbb{R}^n
- 9) the dimension of the row space of A is n
- 10) the rows of A are lin. indep.
- 11) the rows of A span the vector space of row vectors with n entries
- 12) A has an inverse
- 13) $Ax=b$ has a unique solution for all $b \in \mathbb{R}^n$
- 14) $\det A \neq 0$
- 15) $\lambda=0$ is not an eigenvalue for A

2. (10 points) Define "vector space".

The subset V of \mathbb{R}^n is a vector space if it is closed under addition and scalar multiplication.

contains zero and