PRINT Your Name:

## Quiz for June 18, 2012

The quiz is worth 5 points. **Remove EVERYTHING from your desk except** this quiz and a pen or pencil. SHOW your work. Express your work in a neat and coherent manner. BOX your answer.

Find a particular solution of  $y'' - y' - 6y = 2\sin 3x$ .

**ANSWER:** We look for a solution of the form  $y = A \sin 3x + B \cos 3x$ . We compute

$$y' = 3A\cos 3x - 3B\sin 3x$$
$$y'' = -9A\sin 3x - 9B\cos 3x.$$

Plug our candidate into the DE to get

$$-9A\sin 3x - 9B\cos 3x - (-3B\sin 3x + 3A\cos 3x) \\ -6(A\sin 3x + B\cos 3x) \\ \end{vmatrix} = 2\sin 3x$$

We want

$$(-9A + 3B - 6A)\sin 3x + (-9B - 3A - 6B)\cos 3x = 2\sin 3x.$$

We want

$$-15A + 3B = 2-3A - 15B = 0.$$

We want

$$-5A + B = 2/3$$
  
 $-A - 5B = 0.$ 

We want

$$\begin{bmatrix} -5 & 1 \\ -1 & -5 \end{bmatrix} \begin{bmatrix} A \\ B \end{bmatrix} = \begin{bmatrix} 2/3//0 \end{bmatrix}.$$

Multiply both sides of the equation on the left by  $\begin{bmatrix} -5 & -1 \\ 1 & -5 \end{bmatrix}$ . We want

$$\begin{bmatrix} -5 & -1 \\ 1 & -5 \end{bmatrix} \begin{bmatrix} -5 & 1 \\ -1 & -5 \end{bmatrix} \begin{bmatrix} A \\ B \end{bmatrix} = \begin{bmatrix} -5 & -1 \\ 1 & -5 \end{bmatrix} \begin{bmatrix} 2/3 \\ 0 \end{bmatrix}.$$

We want

$$\begin{bmatrix} 26 & 0 \\ 0 & 26 \end{bmatrix} \begin{bmatrix} A \\ B \end{bmatrix} = \begin{bmatrix} -10/3 \\ 2/3 \end{bmatrix}.$$

Take  $A = \frac{-10}{3} \frac{1}{26} = \frac{-5}{39}$  and  $B = \frac{2}{3} \frac{1}{26} = \frac{1}{39}$ . Our answer is

$$y = \frac{-5}{39}\sin 3x + \frac{1}{39}\cos 3x$$