## No calculators, cell phones, computers, notes, etc.

Circle your answer. Make your work correct, complete and coherent.

The quiz is worth 5 points. The solutions will be posted on my website later today.

E-mail your solution to

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## Quiz 7, Monday, March 15, 2021

Find the general solution of y'' + 6y' + 9y = 0.

Answer: We try  $y = e^{rx}$ . We solve the characteristic polynomial  $r^2 + 6r + 9 = 0$ . This polynomial is  $(r+3)^2 = 0$ . So, r = -3 is a root of multiplicity 2. The corresponding solutions of the Differential Equation are  $y = e^{-3x}$  and  $y = xe^{-3x}$ . The general solution of the Differential Equation is

$$y = c_1 e^{-3x} + c_2 x e^{-3x}.$$

Check: We compute

$$y' = -3c_1e^{-3x} + c_2(-3xe^{-3x} + e^{-3x})$$

and

$$y'' = 9c_1e^{-3x} + c_2(9xe^{-3x} - 3e^{-3x} - 3e^{-3x}) = 9c_1e^{-3x} + c_2(9xe^{-3x} - 6e^{-3x}).$$

Plug *y* into the DE to obtain

$$9c_1e^{-3x} + c_2(9xe^{-3x} - 6e^{-3x}) + 6[-3c_1e^{-3x} + c_2(-3xe^{-3x} + e^{-3x})] + 9[c_1e^{-3x} + c_2xe^{-3x}]$$
  
=  $c_1e^{-3x}[9 - 18 + 9] + c_2e^{-3x}[x(9 - 18 + 9) + (-6 + 6)] = 0.\checkmark$