$\qquad$
No calculators, cell phones, computers, notes, etc.
Circle your answer. Make your work correct, complete and coherent.
The quiz is worth 5 points. The solutions will be posted on my website later today.
E-mail your solution to
kustin@math.sc.edu

## Quiz 7, Monday, March 15, 2021

Find the general solution of $y^{\prime \prime}+6 y^{\prime}+9 y=0$.
Answer: We try $y=e^{r x}$. We solve the characteristic polynomial $r^{2}+6 r+9=0$. This polynomial is $(r+3)^{2}=0$. So, $r=-3$ is a root of multiplicity 2 . The corresponding solutions of the Differential Equation are $y=e^{-3 x}$ and $y=x e^{-3 x}$. The general solution of the Differential Equation is

$$
y=c_{1} e^{-3 x}+c_{2} x e^{-3 x}
$$

Check: We compute

$$
y^{\prime}=-3 c_{1} e^{-3 x}+c_{2}\left(-3 x e^{-3 x}+e^{-3 x}\right)
$$

and

$$
y^{\prime \prime}=9 c_{1} e^{-3 x}+c_{2}\left(9 x e^{-3 x}-3 e^{-3 x}-3 e^{-3 x}\right)=9 c_{1} e^{-3 x}+c_{2}\left(9 x e^{-3 x}-6 e^{-3 x}\right)
$$

Plug $y$ into the DE to obtain

$$
\begin{gathered}
9 c_{1} e^{-3 x}+c_{2}\left(9 x e^{-3 x}-6 e^{-3 x}\right)+6\left[-3 c_{1} e^{-3 x}+c_{2}\left(-3 x e^{-3 x}+e^{-3 x}\right)\right]+9\left[c_{1} e^{-3 x}+c_{2} x e^{-3 x}\right] \\
=c_{1} e^{-3 x}[9-18+9]+c_{2} e^{-3 x}[x(9-18+9)+(-6+6)]=0 .
\end{gathered}
$$

