

Please PRINT your name \_\_\_\_\_

**No calculators, cell phones, computers, notes, etc.**

Circle your answer. Make your work correct, complete and coherent.

Please take a picture of your quiz (for your records) just before you turn the quiz in. I will e-mail your grade and my comments to you.

The quiz is worth 5 points. The solutions will be posted on my website later today.

**Math 242, Quiz 2, January 27, 2025**

Solve the Initial Value Problem

$$\frac{dy}{dx} = x\sqrt{x^2 + 9} \quad \text{and} \quad y(-4) = 0.$$

**Solution.** Separate the variables and integrate:

$$\int 1 dy = \int x\sqrt{x^2 + 9} dx.$$

Let  $u = x^2 + 9$ . Then  $du = 2x dx$ . We obtain

$$y = \frac{1}{2} \int u^{\frac{1}{2}} du = \frac{1}{2} \cdot \frac{2}{3} u^{3/2} + C = \frac{1}{3} (x^2 + 9)^{3/2} + C$$

We use the initial condition  $0 = y(-4)$  to find  $C$ :

$$0 = y(-4) = \frac{1}{3} ((-4)^2 + 9)^{3/2} + C = \frac{125}{3} + C$$

So,  $C = -\frac{125}{3}$  and

$$y = \frac{1}{3} (x^2 + 9)^{3/2} - \frac{125}{3}.$$

**Check.** We compute

$$y = \frac{1}{3} (x^2 + 9)^{3/2} - \frac{125}{3}$$

$$y' = \frac{1}{2} (x^2 + 9)^{1/2} 2x \checkmark$$

$$\text{and } y(-4) = \frac{1}{3} (25)^{3/2} - \frac{125}{3} = 0 \checkmark$$