

PRINT Your Name: \_\_\_\_\_

### Quiz 2, Fall, 2012

The quiz is worth 5 points. **Remove EVERYTHING from your desk except this quiz and a pen or pencil.** SHOW your work. Express your work in a neat and coherent manner. BOX your answer. **Check your answer**

Solve the initial value problem  $2y \frac{dy}{dx} = \frac{x}{\sqrt{x^2-16}}$ ,  $y(5) = 2$ .

**Express your answer in the form**  $y = y(x)$ .

**ANSWER:** Multiply both sides by  $dx$  and integrate:  $\int 2y dy = \int \frac{x}{\sqrt{x^2-16}} dx$  to obtain

$$y^2 = \sqrt{x^2 - 16} + C.$$

Plug in  $y(5) = 2$  to see that  $4 = \sqrt{25 - 16} + C$ ; that is,  $4 = 3 + C$  or  $1 = C$ . Thus,

$$y^2 = \sqrt{x^2 - 16} + 1.$$

We solve for  $y$  to learn that

$$y = \pm \sqrt{\sqrt{x^2 - 16} + 1}.$$

However,  $y$  is sometimes positive; so,  $y = \sqrt{\sqrt{x^2 - 16} + 1}$ .

**Check:** Plug in  $x = 5$  to get  $y = \sqrt{\sqrt{25 - 16} + 1} = \sqrt{3 + 1} = 2$ , as desired. Now we take the derivative

$$2y \frac{dy}{dx} = 2 \sqrt{\sqrt{x^2 - 16} + 1} \frac{\frac{2x}{2\sqrt{x^2-16}}}{2\sqrt{\sqrt{x^2-16}+1}} = \frac{x}{\sqrt{x^2-16}},$$

as desired. ✓