No calculators, cell phones, computers, notes, etc.

Circle your answer. Make your work correct, complete and coherent.

The quiz is worth 5 points. The solutions will be posted on my website later today.

Quiz 8, Monday, April 5, 2021

Find the absolute maximum and the absolute minimum values of

$$f(x, y) = 3xy - 6x - 3y + 7$$

on the triangular region with vertices (0,0), (3,0), and (0,5).

Answer: We compute $\frac{\partial f}{\partial x} = 3y - 6$ and $\frac{\partial f}{\partial y} = 3x - 3$. Both partial derivatives are zero at the point (x, y) = (1, 2). This interior critical point might be an absolute extreme point.

We look at the restriction of *f* to the line y = 0 with $0 \le x \le 3$.

$$f|_{y=0}(x) = -6x + 7$$

and the derivative is -6 which is never zero. So the absolute extreme points of the restriction of *f* to the line y = 0 with $0 \le x \le 3$ occur at the end points.

We look at the restriction of *f* to the line x = 0 with $0 \le y \le 5$.

$$f|_{x=0}(y) = -3y + 7$$

and the derivative is -3 which is never zero. So the absolute extreme points of the restriction of *f* to the line x = 0 with $0 \le y \le 5$ occur at the end points.

The line which connects (3,0) to (0,5) is $y = -\frac{5}{3}x + 5$. We look at the restriction of *f* to the line $y = -\frac{5}{3}x + 5$ with $0 \le x \le 3$.

$$f|_{\text{top boundary}}(x) = 3x(-\frac{5}{3}x+5) - 6x - 3(-\frac{5}{3}x+5) + 7 = -5x^2 + 15x - 6x + 5x - 15 + 7$$

The derivative is -10x+15-6+5. The derivative is zero when -10x+14=0; that is when x = 7/5 and y = 8/3.

The extreme points of f on our domain occur at (0,0), (3,0), (0,5), or (7/5,8/3). We plug these points into f:

$$f(0,0) = 7,$$
 absolute maximum

$$f(3,0) = -18 + 7 = -11$$
 absolute minimum

$$f(0,5) = -15 + 7 = -8$$

$$f(7/5,8/3) = 56/5 - 42/5 - 8 + 7 = 9/5$$

$$f(1,2) = 6 - 6 - 6 + 7 = 1$$

The absolute minimum of f on our domain occurs at (3,0,-11). The absolute maximum of f on our domain occurs at (0,0,7).