

Please PRINT your name _____

No calculators, cell phones, computers, notes, etc.

Circle your answer. Make your work correct, complete and coherent.

The quiz is worth 5 points. The solutions will be posted on my website later today.

Quiz 5, September 14, 2020

Find the equation of the plane through the points $P = (1, 1, -1)$, $Q = (2, 0, 7)$, and $R = (0, -2, 1)$. Check your answer.

The vector $\vec{PQ} \times \vec{PR}$ is perpendicular to the plane. We calculate

$$\vec{PQ} \times \vec{PR} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 1 & -1 & 8 \\ -1 & -3 & 2 \end{vmatrix} = \begin{vmatrix} -1 & 8 \\ -3 & 2 \end{vmatrix} \vec{i} - \begin{vmatrix} 1 & 8 \\ -1 & 2 \end{vmatrix} \vec{j} + \begin{vmatrix} 1 & -1 \\ -1 & -3 \end{vmatrix} \vec{k} = 22\vec{i} - 10\vec{j} - 4\vec{k}.$$

The plane is $22(x - 1) - 10(y - 1) - 4(z + 1) = 0$. Divide both sides of the equation by 2 to obtain

$$11(x - 1) - 5(y - 1) - 2(z + 1) = 0$$

or

$$\boxed{11x - 5y - 2z = 8}.$$

Check.

Plug in P : $11(1) - 5(1) - 2(-1) = 8, \checkmark$

Plug in Q : $11(2) - 5(0) - 2(7) = 8. \checkmark$

Plug in R : $11(0) - 5(-2) - 2(1) = 8. \checkmark$