No calculators, cell phones, computers, notes, etc.

Circle your answer. Make your work correct, complete and coherent.

The quiz is worth 5 points. The solutions will be posted on my website later today.

Quiz 3, February 19, 2019

At time t = 0, a particle is located at the point (1,2,3). It travels in a straight line to the point (4,1,4), has speed 2 at (1,2,3), and has constant acceleration $3\overrightarrow{i} - \overrightarrow{j} + \overrightarrow{k}$. Find an equation for the position vector $\overrightarrow{r}(t)$ of the particle at time t.

ANSWER: We are told that

$$\vec{r}''(t) = 3\vec{i} - \vec{j} + \vec{k}$$
$$\vec{r}(0) = \vec{i} + 2\vec{j} + 3\vec{k}$$
$$\vec{r}'(0) = \frac{2}{\sqrt{11}} \left(3\vec{i} - \vec{j} + \vec{k}\right)$$

Integrate to learn that

$$\overrightarrow{\boldsymbol{r}}'(t) = 3t \overrightarrow{\boldsymbol{i}} - t \overrightarrow{\boldsymbol{j}} + t \overrightarrow{\boldsymbol{k}} + \overrightarrow{\boldsymbol{c}}_1.$$

Plug in t = 0:

$$\frac{2}{\sqrt{11}}\left(3\overrightarrow{\boldsymbol{i}}-\overrightarrow{\boldsymbol{j}}+\overrightarrow{\boldsymbol{k}}\right)=\overrightarrow{\boldsymbol{r}}'(0)=\overrightarrow{\boldsymbol{c}}_{1}.$$

Thus,

$$\vec{r}'(t) = \left(3t + \frac{6}{\sqrt{11}}\right)\vec{i} + \left(-t - \frac{2}{\sqrt{11}}\right)\vec{j} + \left(t + \frac{2}{\sqrt{11}}\right)\vec{k}.$$

Integrate again:

$$\vec{r}(t) = \left(3\frac{t^2}{2} + \frac{6}{\sqrt{11}}t\right)\vec{i} + \left(-\frac{t^2}{2} - \frac{2}{\sqrt{11}}t\right)\vec{j} + \left(\frac{t^2}{2} + \frac{2}{\sqrt{11}}t\right)\vec{k} + \vec{c}_2.$$

$$t = 0:$$

Plug in
$$t = 0$$
:

$$\overrightarrow{i} + 2\overrightarrow{j} + 3\overrightarrow{k} = \overrightarrow{r}(0) = \overrightarrow{c}_2.$$

Thus,

$$\overrightarrow{\mathbf{r}} = \left(3\frac{t^2}{2} + \frac{6}{\sqrt{11}}t + 1\right)\overrightarrow{\mathbf{i}} + \left(-\frac{t^2}{2} - \frac{2}{\sqrt{11}}t + 2\right)\overrightarrow{\mathbf{j}} + \left(\frac{t^2}{2} + \frac{2}{\sqrt{11}}t + 3\right)\overrightarrow{\mathbf{k}}.$$