No calculators, cell phones, computers, notes, etc.

Circle your answer. Make your work correct, complete and coherent.

The quiz is worth 5 points. The solutions will be posted on my website later today.

Quiz 12, Wednesday, November 4, 2020

Find the derivative of the function $f(x,y) = 2xy - 3y^2$ at $P_0 = (5,5)$ in the direction of $\overrightarrow{u} = 4\overrightarrow{i} + 3\overrightarrow{j}$.

Answer:

$$D_{\overrightarrow{\boldsymbol{u}}}f|_{P_0} = \overrightarrow{\nabla}f|_{P_0} \cdot \frac{\overrightarrow{\boldsymbol{u}}}{|\overrightarrow{\boldsymbol{u}}|} = (2y\overrightarrow{\boldsymbol{i}} + (2x - 6y)\overrightarrow{\boldsymbol{j}})|_{(5,5)} \cdot \frac{4\overrightarrow{\boldsymbol{i}} + 3\overrightarrow{\boldsymbol{j}}}{5}$$
$$= (10\overrightarrow{\boldsymbol{i}} - 20\overrightarrow{\boldsymbol{j}}) \cdot \frac{4\overrightarrow{\boldsymbol{i}} + 3\overrightarrow{\boldsymbol{j}}}{5} = (2\overrightarrow{\boldsymbol{i}} - 4\overrightarrow{\boldsymbol{j}}) \cdot (4\overrightarrow{\boldsymbol{i}} + 3\overrightarrow{\boldsymbol{j}}) = 8 - 12 = \boxed{-4}.$$