Please PRINT your name _____

No calculators, cell phones, computers, notes, etc.

Circle your answer. Make your work correct, complete and coherent.

The quiz is worth 5 points. The solutions will be posted on my website later today.

Quiz 10, October 7, 2019

The position vector of a particle in the *xy*-plane at time *t* is

$$\overrightarrow{\mathbf{r}}(t) = (t+1)\overrightarrow{\mathbf{i}} + (t^2-1)\overrightarrow{\mathbf{j}}.$$

- (a) Eliminate the parameter and find an equation in *x* and *y* whose graph is the path of the particle.
- (b) Find the velocity vector of the particle at t = 1.
- (c) Find the acceleration vector of the particle at t = 1.

ANSWER:

(a) We are given x = t + 1 and $y = t^2 - 1$. We eliminate t by dropping x - 1 = t into $y = t^2 - 1$. We obtain $y = (x - 1)^2 - 1$.

(b) The velocity of the particle at time *t* is $\overrightarrow{\mathbf{v}}(t) = \overrightarrow{\mathbf{i}} + 2t \overrightarrow{\mathbf{j}}$. The velocity of the particle at time t = 1 is $|\overrightarrow{\mathbf{v}}(1) = \overrightarrow{\mathbf{i}} + 2\overrightarrow{\mathbf{j}}|$.

(c) The acceleration of the particle at time t is $\overrightarrow{a}(t) = 2\overrightarrow{j}$. The velocity of the particle at time t = 1 is $|\overrightarrow{a}(1) = 2\overrightarrow{j}|$.