$\qquad$

## No calculators, cell phones, computers, notes, etc.

Circle your answer. Make your work correct, complete and coherent.
The quiz is worth 5 points. The solutions will be posted on my website later today.

## Quiz 10, October 7, 2019

The position vector of a particle in the $x y$-plane at time $t$ is

$$
\vec{r}(t)=(t+1) \overrightarrow{\boldsymbol{i}}+\left(t^{2}-1\right) \overrightarrow{\boldsymbol{j}} .
$$

(a) Eliminate the parameter and find an equation in $x$ and $y$ whose graph is the path of the particle.
(b) Find the velocity vector of the particle at $t=1$.
(c) Find the acceleration vector of the particle at $t=1$.

## ANSWER:

(a) We are given $x=t+1$ and $y=t^{2}-1$. We eliminate $t$ by dropping $x-1=t$ into $y=t^{2}-1$. We obtain $y=(x-1)^{2}-1$.
(b) The velocity of the particle at time $t$ is $\overrightarrow{\boldsymbol{v}}(t)=\overrightarrow{\boldsymbol{i}}+2 t \overrightarrow{\boldsymbol{j}}$. The velocity of the particle at time $t=1$ is $\overrightarrow{\boldsymbol{v}}(1)=\overrightarrow{\boldsymbol{i}}+2 \overrightarrow{\boldsymbol{j}}$.
(c) The acceleration of the particle at time $t$ is $\overrightarrow{\boldsymbol{a}}(t)=2 \overrightarrow{\boldsymbol{j}}$. The velocity of the particle at time $t=1$ is $\overrightarrow{\boldsymbol{a}}(1)=2 \overrightarrow{\boldsymbol{j}}$.

