

# Math 241 Fall 2001 Final

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PRINT Your Name: \_\_\_\_\_

Get your course grade from TIPS/VIP late on Tuesday or later.

There are 18 problems on 10 pages. The exam is worth a total of 150 points.

SHOW your work. **CIRCLE** your answer. NO CALCULATORS!

1. (8 points) Find the equation of the plane through  $(2, 1, 2)$ ,  $(2, -1, 1)$ , and  $R = (4, 0, 0)$ . **CHECK YOUR ANSWER!**  $P =$   $Q =$

$$\overrightarrow{PQ} = -2\hat{i} - \hat{j}$$

$$\overrightarrow{PR} = 2\hat{i} - \hat{j} - 2\hat{k}$$

$$\overrightarrow{PQ} \times \overrightarrow{PR} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & -2 & -1 \\ 2 & -1 & 1 \end{vmatrix} = 3\hat{i} - 2\hat{j} + 4\hat{k}$$

$$3(x-4) - 2y + 4z = 0$$

$$(3x - 2y + 4z = 12)$$

check at  $P$   $3(2) - 2(1) + 4(2) = 12 \checkmark$

at  $Q$   $3(2) - 2(-1) + 4(1) = 12 \checkmark$

at  $R$   $3(4) + 0 + 0 = 12 \checkmark$

2. (8 points) Find the equations of the line through  $(1, 2, 3)$  and  $(4, 6, 1)$ . **CHECK YOUR ANSWER!**  $P =$   $Q =$

$$\overrightarrow{PQ} = 3\hat{i} + 4\hat{j} - 2\hat{k}$$

$$x = 1 + 3t$$

$$y = 2 + 4t$$

$$z = 3 - 2t$$

check at  $t=0$   $(1, 2, 3) \checkmark$

at  $t=1$   $(4, 6, 1) \checkmark$