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14. Compute $\int_C 2x \, dx - y^3 \, dy$ where C is the line segment from $(1, 2)$ to $(5, 4)$.

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slope $\frac{1}{2}$

$$y - 2 = \frac{1}{2}(x - 1)$$

$$2y - 4 = x - 1$$

Let $x = t$
 $y = \frac{t}{2} + \frac{3}{2}$

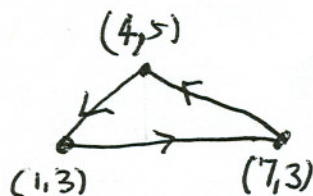
$$1 \leq t \leq 5$$

$$\text{ans} = \int_1^5 \left[2t - \left(\frac{t}{2} + \frac{3}{2} \right)^3 \frac{1}{2} \right] dt$$

$$= \left[t^2 - \frac{\left(\frac{t}{2} + \frac{3}{2} \right)^4}{4} \right]_1^5$$

$$= \left(25 - \frac{(4)^4}{4} - 1 + \frac{(2)^4}{4} \right)$$

15. Compute $\int_C 2y \, dx - 5x \, dy$ where C consists of three line segments. The first line segment for C starts at $(1, 3)$ and goes to $(7, 3)$; the second segment is from $(7, 3)$ to $(4, 5)$; and the third segment is from $(4, 5)$ to $(1, 3)$.



use Green's Thm $\text{ans} = \iint_{\text{region}} (N_x - M_y) \, dA$

$$= \iint_{\text{region}} (5 - 2) \, dA = -7 \text{ area of region}$$

$$= -7 \left(\frac{1}{2} \right) \text{base} \cdot \text{ht} = -7 \left(\frac{1}{2} \right) (6) (2) = \boxed{-42}$$

