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3. Find the equations of any line which is parallel to  $2x - 3y + 4z = 12$ .

$(0,0,0)$  is not on the plane  
 $3\vec{i} + 2\vec{j}$  is  $\parallel$  to the plane

$$\begin{cases} x = 3t \\ y = 2t \\ z = 0 \end{cases}$$

4. Find the equations of the plane tangent to  $z = x^2 + y^2$  when  $x = 1$  and  $y = 2$ .

the point is  $(1, 2, 5)$

$\vec{\nabla}$  are  $\perp$  level sets

my surface is the level set

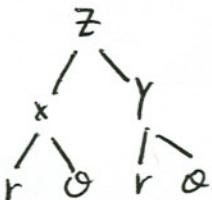
$$0 = x^2 + y^2 - z$$

The relevant  $\vec{\nabla}$  is  $2x\vec{i} + 2y\vec{j} - \vec{k}$

$$\vec{\nabla}|_{pt} = 2\vec{i} + 4\vec{j} - \vec{k}$$

tan plane is  $(2(x-1) + 4(y-2) - (z-5)) = 0$

5. Suppose that  $z = f(x, y)$ , and  $x$  and  $y$  are written polar coordinates (that is,  $x = r \cos \theta$  and  $y = r \sin \theta$ ). Express  $\frac{\partial z}{\partial \theta}$  in terms of  $\frac{\partial z}{\partial x}$  and  $\frac{\partial z}{\partial y}$ .



$$\frac{\partial z}{\partial \theta} = \frac{\partial z}{\partial x}(-r \sin \theta) + \frac{\partial z}{\partial y} r \cos \theta$$