

4. (There is no partial credit for this problem. Make sure your answer is correct.) Find the equation of the plane through $(1, 0, 1)$, $(2, 2, 3)$, and $(3, 5, 6)$.

The perpendicular vector is $\begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 1 & 2 & 2 \\ 2 & 5 & 5 \end{vmatrix}$

$$= 0\vec{i} - \vec{j} + \vec{k}$$

The plane is

$$0(x-1) - (y-0) + (z-1) = 0$$

$$-y + z = 1$$

5. Let $\vec{a} = 3\vec{i} + 2\vec{j}$ and $\vec{b} = \vec{i} - 2\vec{j} + 3\vec{k}$. Compute $\vec{a} \times \vec{b}$.

$$\vec{a} \times \vec{b} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 3 & 2 & 0 \\ 1 & -2 & 3 \end{vmatrix} = (6\vec{i} - 9\vec{j} - 8\vec{k})$$

6. Let $\vec{a} = 3\vec{i} + 2\vec{j}$ and $\vec{b} = \vec{i} - 2\vec{j} + 3\vec{k}$. Find the angle between \vec{a} and \vec{b} .

$$\vec{a} \cdot \vec{b} = \|\vec{a}\| \|\vec{b}\| \cos \theta$$

$$\cos \theta = \frac{\vec{a} \cdot \vec{b}}{\|\vec{a}\| \|\vec{b}\|} = \frac{-1}{\sqrt{13} \sqrt{14}}$$

$$\theta = \cos^{-1} \left(\frac{-1}{\sqrt{13} \sqrt{14}} \right)$$