Math 241, Exam 1, Fall, 2024

You should KEEP this piece of paper. Write everything on the blank paper provided. Return the problems in order (use as much paper as necessary), use only one side of each piece of paper. Number your pages and write your name on each page. Take a picture of your exam (for your records) just before you turn the exam in. I will e-mail your grade and my comments to you. (I will return your exam in the next class.) Fold your exam in half before you turn it in.

The exam is worth 50 points. Each problem is worth 10 points. **Make your work coherent, complete, and correct.** Please *CIRCLE* your answer. Please **CHECK** your answer whenever possible.

The solutions will be posted later today.

No Calculators, Cell phones, computers, notes, etc.

- (1) Find a system of parametric equations for the line through the points $P_1=(4,5,6)$ and $P_2=(3,2,1)$. Check your answer. Make sure it is correct.
- (2) Find an equation for the plane through the points $P_1=(1,1,1)$, $P_2=(-1,2,1)$, and $P_3=(-2,1,2)$. Check your answer. Make sure it is correct.
- (3) Express $\overrightarrow{v} = 2\overrightarrow{i} + 4\overrightarrow{j}$ as the sum of a vector parallel to $\overrightarrow{b} = \overrightarrow{i} + \overrightarrow{j}$ and a vector perpendicular to \overrightarrow{b} . Check your answer. Make sure it is correct.
- (4) Name, describe, and graph the set of all points in three-space which satisfy $x^2 + z^2 = 1$. Is this object a finite set of points, or a curve, or a surface, or a solid?
- (5) Find the point on the plane x + 2y + 3z = 10 that is closest to the point (5,6,7). Check your answer. Make sure it is correct.