

12.4, number 1: Find the length and direction of  $\vec{u} \times \vec{v}$  and  $\vec{v} \times \vec{u}$  for  $\vec{u} = 2\vec{i} - 2\vec{j} - \vec{k}$  and  $\vec{v} = \vec{i} - \vec{k}$ .

**Answer:**

$$\begin{aligned}\vec{u} \times \vec{v} &= \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 2 & -2 & -1 \\ 1 & 0 & -1 \end{vmatrix} = \begin{vmatrix} -2 & -1 \\ 0 & -1 \end{vmatrix} \vec{i} - \begin{vmatrix} 2 & -1 \\ 1 & -1 \end{vmatrix} \vec{j} + \begin{vmatrix} 2 & -2 \\ 1 & 0 \end{vmatrix} \vec{k} \\ &= 2\vec{i} + \vec{j} + 2\vec{k}.\end{aligned}$$

The length of  $\vec{u} \times \vec{v}$  is  $\sqrt{2^2 + 1^2 + 2^2} = \boxed{3}$  and the unit vector that has the same direction as  $\vec{u} \times \vec{v}$  is  $\boxed{\frac{1}{3}(2\vec{i} + \vec{j} + 2\vec{k})}$ . It follows that the length of  $\vec{v} \times \vec{u}$  is also  $\boxed{3}$  and a unit vector that points in the same direction as  $\vec{v} \times \vec{u}$  is  $\boxed{\frac{-1}{3}(2\vec{i} + \vec{j} + 2\vec{k})}$ .

You can compute the second half of the answer or just state the second half of the answer, which ever feels better to you.