

PRINT Your Name: _____

There are 10 problems on 4 pages. Each problem is worth 10 points.

CIRCLE your answers.

1. True or False. If true, **prove** it. If false, then give a **counterexample**. A necessary condition for an integer to be divisible by 6 is that it be divisible by 2.

(p is a necessary condition for q) $\equiv (q \rightarrow p)$
 In this problem $p =$ the integer is divisible by 2
 $q =$ the integer is divisible by 6

so the problem asks:

$$\text{T/F } 6|n \Rightarrow 2|n$$

This is **True**

If $6 \nmid n$, then $n = 6k$ for some integer k . Thus
 $n = 2 \cdot 3k$ thus $2|n$.

2. True or False. If true, **prove** it. If false, then give a **counterexample**. The sum of any two irrational numbers is irrational.

False $\sqrt{2}$ is irrational, $-\sqrt{2}$ is irrational
 but $\sqrt{2} + (-\sqrt{2}) = 0$ which is rational.