

Name:

HW 3: §C.1-C.3

Complete the following problems to the best of your ability. **SHOW ALL OF YOUR WORK.** Unshown work will not be graded. You may use a calculator.

1. Solve the following equations for  $x$ .

(a)  $2x - 4 = 7$   $x = \frac{11}{2}$   
 $2x = 11$

(b)  $\left(\frac{x}{3} - \frac{1}{2}\right)6 = -\frac{2}{3}$   
 $2x - 3 = -4 \rightarrow 2x = -1 \rightarrow x = -\frac{1}{2}$

(c)  $x^2 - 9 = -5$   
 $x^2 = 4$   
 $x = \pm 2$

(d)  $\sqrt[3]{x} = 4$   
 $x = 4^3 = 64$

(e)  $x^2 = 3x - 2$   
 $x^2 - 3x + 2 = 0 \rightarrow (x-2)(x-1) = 0 \quad \text{so } x = 1, 2$

(f)  $4 = -x^2 + 4x$   
 $x^2 - 4x + 4 = 0$   
 $(x-2)(x-2) = 0$   
 $\text{so } x = 2$

2. Solve the equation  $x^2 - 4x + 2 = 0$  by completing the square.

$$\begin{aligned} x^2 - 4x + 2 &= 0 & \rightarrow (x-2)^2 &= 2 \\ x^2 - 4x + 4 - 4 + 2 &= 0 & x-2 &= \pm \sqrt{2} \\ (x-2)^2 - 2 &= 0 & x &= 2 \pm \sqrt{2} \end{aligned}$$

3. Solve the equation  $3x^2 + 6x - 5 = 0$  by using the quadratic formula.

$$\begin{aligned} a &= 3 & x &= \frac{-6 \pm \sqrt{36 - 4(3)(-5)}}{2(3)} = \frac{-6 \pm \sqrt{36 + 60}}{6} = -1 \pm \frac{\sqrt{96}}{6} \\ b &= 6 & & \\ c &= -5 & & \end{aligned}$$

4. Solve the following inequalities for  $x$ .

(a)  $5 \leq 3x - 4 < 14$   
+4      +4      +4

$$\frac{9}{3} \leq \frac{3x}{3} < \frac{18}{3}$$

$$3 \leq x < 6$$

(b)  $x^2 \geq 9$  (be careful with this one!)

$$\begin{aligned} x^2 - 9 &\geq 0 \\ (x-3)(x+3) &\geq 0 \end{aligned} \quad \text{so } (-\infty, -3] \cup [3, \infty)$$

$$\begin{array}{c} + \quad - \quad + \\ \leftarrow \quad \quad \quad \rightarrow \\ -3 \quad \quad \quad 3 \end{array}$$

Optional Problems:

- C.1: All
- C.2: 1-36
- C.3: 1, 2, 11-34