

On this homework (provided your specifically reference it when used) you may use the following Theorem from class.

Nested Interval Property. (Really a Theorem).

Let $(I_n)_{n=1}^{\infty}$ be a sequence of nonempty closed bounded intervals of \mathbb{R} that are nested in the sense

$$I_{j+1} \subseteq I_j \quad \text{for each } j \in \mathbb{N}.$$

Then

$$(1) \quad \bigcap_{n=1}^{\infty} I_n \text{ is nonempty,}$$

$$(2) \quad \text{and if furthermore the } \lim_{n \rightarrow \infty} \text{length}(I_n) = 0 \text{ then } \bigcap_{n=1}^{\infty} I_n \text{ has precisely one element.}$$

Variant of book's ER 2.5.9

§2.5
BS4p52

1. For each $n \in \mathbb{N}$, let

$$K_n := [n, \infty).$$

Prove that $\bigcap_{n=1}^{\infty} K_n = \emptyset$.

2. In the above statement of the **Nested Interval Property**, can the assumption that the intervals are bounded be omitted? Justify your answer.

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