

Specifically say where you are using Archimedean's Property (or one of it's corollaries) when you use it. Below is a list of the versions of Archimedean's Property that we showed in class.

Thm AP. (Archimedean's Property) $(\forall b \in \mathbb{R}) (\forall a \in \mathbb{R}^{>0}) (\exists n \in \mathbb{N}) [b < na]$

Cor. 1. $(\forall x \in \mathbb{R}) (\exists n \in \mathbb{N}) [x < n]$

Cor. 2. $(\forall \varepsilon > 0) (\exists n \in \mathbb{N}) [\frac{1}{n} < \varepsilon]$

Cor. 3. $(\forall z \in \mathbb{R}^{>0}) (\exists n \in \mathbb{N}) [n - 1 \leq z < n]$

Variant of book's ER 2.4.2

§2.4
BS4p44

Let

$$D = \left\{ \frac{1}{j} - \frac{1}{k} : j, k \in \mathbb{N} \right\} .$$

- 1a. Conjecture the sup D .
- 1b. Prove your conjecture in 1a is true.
- 2a. Conjecture the inf D .
- 2b. Prove your conjecture in 2a is true.

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