

Henceforth, when asked to *symbolically write* a statement follow the below (unless otherwise stated).

- (1) If a statement is a quantified open sentence, then use needed quantifier(s) (e.g.: \forall , \exists , $\exists!$).

Recall

- \forall reads *for all*
- \exists reads *there exists*
- $\exists!$ reads *there exists a unique*.

- (2) Use logical connectives symbols (e.g.: \sim , \wedge , \vee , \implies , \iff) instead of the English words.

- (3) Within an open sentence, you can use English words that are not logical connectives words.

E.g., within your open sentence, one can write: “ x is even”.

Beware: “ x and y are odd” should be expressed as “ x is odd \wedge y is odd”.

- (4) Within an open sentence, you can use math symbols that are not logical connectives.

So you may use, e.g.: $x < \sqrt{2}$, $x = y$, $x + y = 17$, $a|b$, $a \equiv b \pmod{n}$, $\sum_{j=1}^n j^2 = \frac{n(n+1)(2n+1)}{6}$.

- (5) Symbolically write the statement as it is stated (rather than something logically equivalent).

For example, the statement

$$\text{if a real number is larger than 3, then its square is larger than 9} \quad (1)$$

can be symbolically written as

$$(\forall x \in \mathbb{R}) [x > 3 \implies x^2 > 9] . \quad (\text{yes})$$

The statement in (1) is formulated as in (yes) so symbolically write (1) as (yes).

Do NOT symbolically write the statement in (1) as

$$(\forall x \in \mathbb{R}) [x^2 \leq 9 \implies x \leq 3] \quad (\text{no})$$

since (no) is not as (1) is formulated. Do note (will help you later) that the statement in (yes)

is logically equivalent to the statement in (no) (since $[P \implies Q] \equiv [(\sim Q) \implies (\sim P)]$, think

contrapositive); thus, if you need to prove the statement in (1), then you can prove (yes)

OR (no) (choice is yours when proving).