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(a) $\begin{aligned} x &= 2 - 9t \\ y &= 9 + 6t \\ z &= 8 - 2t \end{aligned}$

(b) $\begin{aligned} x &= 24 + 18t \\ y &= 12 - 12t \\ z &= 8 + 4t \end{aligned}$

(c) $\begin{aligned} x &= 20 + 18t \\ y &= -3 - 12t \\ z &= 10 + 4t \end{aligned}$

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