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Overview

The objective of this lab is to provide some Maple tools to help you practice integration skills, such as integration by substitution and integration by parts.

Maple Essentials

• Important Maple commands introduced in this lab:

Command/Example	Description
Hint(Expression);	returns Hints for a calculus problem matching
Examples:	the Expression which is typically in form of
<pre>Hint(Int(f(x),x));</pre>	Diff(), Int(), or Limit(). Note:
Note: You need to load the	The first letter of Hint, Diff, Int, and Limit must
Student[Calculus1] package before us-	be capitalized.
ing this command.	
Rule[rule](Expression);	used to apply a rule obtained from Hint to a
Examples:	matching problem.
<pre>Rule[parts,U,V](Int(f(x),x));</pre>	Note: It is often easier to use names and equation la-
Rule[h1](Int(f(x),x));	bels as inputs. In the last two examples, we assign our
Rule[h1[2]](Int(f(x),x));	hint to h1.

Maple is very capable when evaluating integrals, derivatives, and limits, but if you want to see individual steps or methods to be applied for such calculus problems (rather than just final answers), you need to use commands Hint and Rule. However, there are a few things that you should know:

- 1. There are many different ways to do a calculus problem and Maple's way may be different from yours. While Maple in general will give good hints, you may find a different or better way to do the problem.
- 2. Because of the constant C in integral formulas, your final answer to an indefinite integral may look different from the one given by Maple. The best way to be sure that the both are correct is to take the derivative of the difference to see if it equals zero.
- 3. Maple may use methods that we have not learned yet.
- 4. Maple should be used as a tool to facilitate your learning. Remember, you will need to be able to evaluate these integrals by hand. Do not rely too heavily on Maple.
- The Integration by Substitution maplet is available from the course website:

 $\rm http://www.math.sc.edu/calclab/142L-S12/labs \rightarrow \underline{\rm Integration \ by \ Substitution}$

This maplet is designed to help you practice the steps involved in integration by substitution. Click on **Indefinite Integral** or **Definite Integral** to have the maplet generate a problem for you to practice. For a definite integral, you will be asked to calculate the associated indefinite integral first. You can then choose to change the limits of integration or substitute to return to the original variable. You can click **Hint** or **Show** if you need help or want to skip a step.

• The Integration by Parts maplet is available from the course website: http://www.math.sc.edu/calclab/142L-S12/labs → Integration by Parts

This maplet is designed to help you practice the steps involved in integration by parts. Its interface is very similar to the last maplet.

Related course material

Stewart Text: $\S5.5$ and $\S7.1.$ Maple Text: $\S6.3$ and $\S6.4.$

Activities

- 1. Launch Integration by Substitution maplet from the course web page and do a few practice problems.
- 2. Launch Integration by Parts maplet from the course web page and do a few practice problems.
- 3. Use Maple to help you to evaluate the following:

(a)
$$\int \sin x \cos^6 x \, dx$$

(b)
$$\int x^5 \ln x \, dx$$

(c)
$$\int x \sin x \, dx$$

(d)
$$\int \frac{x^2 + 1}{\sqrt{x^3 + 3x + 1}} \, dx$$

(e)
$$\int \sin^{-1} x \, dx$$

(f)
$$\int xe^x \, dx$$

Example Problem

Evaluate $\int t^3 e^{-t^2} dt$. (Exercise 34 on page 458)

- 1. Start a Maple session and don't forget to load Student[Calculus1] package. > with(Student[Calculus1]):
- 2. Assign expression to be integrated as a function f(t). > f:=t -> t^3*exp(-t^2);
- 3. Apply Hint and assign the hint to h1.

> h1:=Hint(Int(f(t),t));

The return suggests to use parts with $U = t^2$ and $V = -\frac{1}{2}e^{-t^2}$ or a substitution with $U = t^2$. Notice that $U = t^3$ won't work for parts since $V = \int e^{-t^2} dx$ cannot be evaluated.

- 4. To apply the first hint, enter the following: > Rule[h1](Int(f(t),t));
- 5. To apply the second hint, enter the following: > Rule[h1[2]](Int(f(t),t));
- 6. You should be able to complete the problem by hand after seeing the hint applied, but you may continue to receive and apply hints using the equation labels if you need to.

Assignment

With the help of Maple, work out the problems assigned by your lab instructor. Clearly identify your answers on your Maple worksheet. Make sure you answer each question completely. Your assignment is due at the **beginning** of next week's lab.