Differentiate each of the following by hand.

1.
$$f(x) = \frac{x}{1 - \ln(x - 1)}$$

$$2. \ y = \frac{\ln\left(\ln(x)\right)}{2}$$

3.
$$f(t) = \ln(t^3 - e^{4t} + 3)$$

4.
$$f(x) = \log_{10}(x\sqrt{x^2 - 1})$$

5.
$$h(t) = t \ln(t) - t$$

6.
$$f(x) = 3x \log_5(\sqrt{x})$$

7.
$$S(x) = \ln\left(\frac{(2x+1)^5}{\sqrt{x^2-1}}\right)$$