

MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AN QUOTIENT RULES

MATH 122

Ann Clifton 1

¹University of South Carolina, Columbia, SC USA

Calculus for Business Administration and Social Sciences



OUTLINE

MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

1 3.3: THE CHAIN RULE



OUTLINE

MATH 122

CLIFTO

3.3: THE CHAIN RULI

7.4: THE PRODUCT AN QUOTIENT RULES

1 3.3: THE CHAIN RULE

2 3.4: The Product and Quotient Rules



THE CHAIN RULE

MATH 122

CLIFTO

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

THEOREM 1

Let f and g be differentiable functions such that $f \circ g(x)$ is well-defined.



THE CHAIN RULE

MATH 122

CLIFTON

3.3: THE CHAIN RULE

PRODUCT AN QUOTIENT RULES

THEOREM 1

Let f and g be differentiable functions such that $f \circ g(x)$ is well-defined. The derivative of the composition is given by

$$(f \circ g)'(x) = (f' \circ g(x)) \cdot g'(x).$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AND QUOTIENT RULES

Let
$$P(t) = P_0 a^t$$
.



MATH 122

CLIFTON

3.3: THE CHAIN RULE

5.4: THE PRODUCT AN QUOTIENT RULES

Let
$$P(t) = P_0 a^t$$
.
Let $f(t) = P_0 e^t$ and let $g(t) = \ln(a)t$ so $(f \circ g)(t)$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

9.4: THE
PRODUCT AN
QUOTIENT
RULES

Let
$$P(t) = P_0 a^t$$
.
Let $f(t) = P_0 e^t$ and let $g(t) = \ln(a)t$ so

$$(f\circ g)(t)=f(\ln(a)t)$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Let $P(t) = P_0 a^t$. Let $f(t) = P_0 e^t$ and let $g(t) = \ln(a)t$ so

$$(f\circ g)(t)=f(\ln(a)t)=P_0e^{\ln(a)t}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Let
$$P(t) = P_0 a^t$$
.
Let $f(t) = P_0 e^t$ and let $g(t) = \ln(a)t$ so
$$(f \circ g)(t) = f(\ln(a)t) = P_0 e^{\ln(a)t} = P_0 (e^{\ln(a)})^t$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Let $P(t) = P_0 a^t$. Let $f(t) = P_0 e^t$ and let $g(t) = \ln(a)t$ so

$$(f \circ g)(t) = f(\ln(a)t) = P_0 e^{\ln(a)t} = P_0 (e^{\ln(a)})^t = P_0 a^t$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Let
$$P(t) = P_0 a^t$$
.
Let $f(t) = P_0 e^t$ and let $g(t) = \ln(a)t$ so

$$(f \circ g)(t) = f(\ln(a)t) = P_0e^{\ln(a)t} = P_0(e^{\ln(a)})^t = P_0a^t = P(t).$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Let $P(t) = P_0 a^t$. Let $f(t) = P_0 e^t$ and let $g(t) = \ln(a)t$ so

$$(f \circ g)(t) = f(\ln(a)t) = P_0e^{\ln(a)t} = P_0(e^{\ln(a)})^t = P_0a^t = P(t).$$

$$P'(t) = f' \circ g(t) \cdot g'(t)$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

PRODUCT AN QUOTIENT RULES Let $P(t) = P_0 a^t$. Let $f(t) = P_0 e^t$ and let $g(t) = \ln(a)t$ so

$$(f \circ g)(t) = f(\ln(a)t) = P_0 e^{\ln(a)t} = P_0 (e^{\ln(a)})^t = P_0 a^t = P(t).$$

$$P'(t) = f' \circ g(t) \cdot g'(t)$$

= $P_0 e^{\ln(a)t} \cdot \ln(a)$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

PRODUCT AN QUOTIENT RULES Let $P(t) = P_0 a^t$. Let $f(t) = P_0 e^t$ and let $g(t) = \ln(a)t$ so

$$(f \circ g)(t) = f(\ln(a)t) = P_0e^{\ln(a)t} = P_0(e^{\ln(a)})^t = P_0a^t = P(t).$$

$$P'(t) = f' \circ g(t) \cdot g'(t)$$

$$= P_0 e^{\ln(a)t} \cdot \ln(a)$$

$$= P_0 a^t \cdot \ln(a)$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

5.4: THE PRODUCT AN QUOTIENT RULES Let $P(t) = P_0 a^t$. Let $f(t) = P_0 e^t$ and let $g(t) = \ln(a)t$ so

$$(f \circ g)(t) = f(\ln(a)t) = P_0 e^{\ln(a)t} = P_0 (e^{\ln(a)})^t = P_0 a^t = P(t).$$

$$P'(t) = f' \circ g(t) \cdot g'(t)$$

$$= P_0 e^{\ln(a)t} \cdot \ln(a)$$

$$= P_0 a^t \cdot \ln(a)$$

$$= \ln(a)P(t).$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AND QUOTIENT RULES

Differentiate $(x + 5)^2$.



MATH 122

CLIFTOR

3.3: THE CHAIN RULE

3.4: THE PRODUCT ANI QUOTIENT RULES

Differentiate $(x + 5)^2$.

First we identify this function as a composition.



MATH 122

Differentiate $(x + 5)^2$.

3.3: THE CHAIN RULE First we identify this function as a composition. If we let f(x) =___ and g(x) =____, then $f \circ g(x) = (x+5)^2$.

3.4: THE PRODUCT AN QUOTIENT RULES



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Differentiate $(x + 5)^2$.



MATH 122

3.3: THE CHAIN RULE

3.4: THE
PRODUCT AN
QUOTIENT
RULES

Differentiate $(x + 5)^2$.

•
$$f'(x) = 2x$$
.



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- g'(x) =



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) =$



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) =$



Матн 122

3.3: THE CHAIN RULE

3.4: THE
PRODUCT AN
QUOTIENT
RULES

Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 =$



MATH 122

3.3: THE CHAIN RULE

3.4: THE
PRODUCT AN
QUOTIENT
RULES

Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 = 1.$



MATH 122

3.3: THE CHAIN RULE

3.4: THE
PRODUCT AN
QUOTIENT
RULES

Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 = 1.$
- $f' \circ g(x) =$



MATH 122

3.3: The

3.4: THE PRODUCT AN QUOTIENT RULES

CHAIN RULE

Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 = 1.$
- $f' \circ g(x) = f'(g(x)) =$



Матн 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 = 1.$
- $f' \circ g(x) = f'(g(x)) = f'(x+5) =$



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 = 1.$
- $f' \circ g(x) = f'(g(x)) = f'(x+5) = 2(x+5) =$



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 = 1.$
- $f' \circ g(x) = f'(g(x)) = f'(x+5) = 2(x+5) = 2x+10.$



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 = 1.$
- $f' \circ g(x) = f'(g(x)) = f'(x+5) = 2(x+5) = 2x+10.$
- Therefore by the Chain Rule

$$\frac{d}{dx}(x+5)^2 =$$



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 = 1.$
- $f' \circ g(x) = f'(g(x)) = f'(x+5) = 2(x+5) = 2x+10.$
- Therefore by the Chain Rule

$$\frac{d}{dx}(x+5)^2 = \frac{d}{dx}(f \circ g(x)) =$$



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 = 1.$
- $f' \circ g(x) = f'(g(x)) = f'(x+5) = 2(x+5) = 2x+10.$
- Therefore by the Chain Rule

$$\frac{\mathrm{d}}{\mathrm{d}x}(x+5)^2 = \frac{\mathrm{d}}{\mathrm{d}x}(f\circ g(x)) = (f'\circ g(x))\cdot g'(x)$$



MATH 122

3.3: THE CHAIN RULE

3.4: THE
PRODUCT AN
QUOTIENT
RULES

Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 = 1.$
- $f' \circ g(x) = f'(g(x)) = f'(x+5) = 2(x+5) = 2x+10.$
- Therefore by the Chain Rule

$$\frac{d}{dx}(x+5)^2 = \frac{d}{dx}(f \circ g(x)) = (f' \circ g(x)) \cdot g'(x)$$
$$= (2x+10) \cdot 1$$



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(x + 5)^2$.

- f'(x) = 2x.
- $g'(x) = \frac{d}{dx}(x+5) = \frac{d}{dx}(x) + \frac{d}{dx}(5) = 1 + 0 = 1.$
- $f' \circ g(x) = f'(g(x)) = f'(x+5) = 2(x+5) = 2x+10.$
- Therefore by the Chain Rule

$$\frac{d}{dx}(x+5)^2 = \frac{d}{dx}(f \circ g(x)) = (f' \circ g(x)) \cdot g'(x)$$

$$= (2x+10) \cdot 1$$

$$= 2x+10.$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AND QUOTIENT RULES

Differentiate e^{3x} .



MATH 122

CLIFTON

3.3: THE CHAIN RULE

PRODUCT AND QUOTIENT RULES

Differentiate e^{3x} .

First we identify this function as a composition.



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Differentiate e^{3x} .

First we identify this function as a composition. If we let f(x) =__ and g(x) =__, then $f \circ g(x) = e^{3x}$.



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Differentiate e^{3x} .



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Differentiate e^{3x} .

•
$$f'(x) = e^x$$
.



MATH 122

3.3: THE CHAIN RULE

PRODUCT AN QUOTIENT RULES

Differentiate e^{3x} .

- $f'(x) = e^x$.
- g'(x) =



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) =$



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) =$



MATH 122

3.3: THE CHAIN RULE

3.4: THE
PRODUCT AN
QUOTIENT
RULES

Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) = 3(1) =$



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) = 3(1) = 3.$



Матн 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) = 3(1) = 3.$
- $f' \circ g(x) =$



Матн 122

3.3: THE CHAIN RULE

5.4: THE PRODUCT AN QUOTIENT RULES Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) = 3(1) = 3.$
- $f' \circ g(x) = f'(g(x)) =$



Матн 122

3.3: THE CHAIN RULE

3.4: THE
PRODUCT AN
QUOTIENT
RULES

Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) = 3(1) = 3.$
- $f' \circ g(x) = f'(g(x)) = f'(3x) =$



Матн 122

3.3: THE CHAIN RULE

3.4: THE
PRODUCT AN
QUOTIENT
RULES

Differentiate e^{3x} .

- $\bullet \ f'(x) = e^x.$
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) = 3(1) = 3.$
- $f' \circ g(x) = f'(g(x)) = f'(3x) = e^{3x}$.



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) = 3(1) = 3.$
- $f' \circ g(x) = f'(g(x)) = f'(3x) = e^{3x}$.
- Therefore by the Chain Rule

$$\frac{d}{dx}\left(e^{3x}\right) =$$



MATH 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) = 3(1) = 3.$
- $f' \circ g(x) = f'(g(x)) = f'(3x) = e^{3x}$.
- Therefore by the Chain Rule

$$\frac{d}{dx}\left(e^{3x}\right) = \frac{d}{dx}\left(f\circ g(x)\right) =$$



Матн 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) = 3(1) = 3.$
- $f' \circ g(x) = f'(g(x)) = f'(3x) = e^{3x}$.
- Therefore by the Chain Rule

$$\frac{d}{dx}\left(e^{3x}\right) = \frac{d}{dx}\left(f\circ g(x)\right) = \left(f'\circ g(x)\right)\cdot g'(x)$$



Матн 122

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) = 3(1) = 3.$
- $f' \circ g(x) = f'(g(x)) = f'(3x) = e^{3x}$.
- Therefore by the Chain Rule

$$\frac{d}{dx}\left(e^{3x}\right) = \frac{d}{dx}\left(f \circ g(x)\right) = \left(f' \circ g(x)\right) \cdot g'(x)$$
$$= e^{3x} \cdot 3$$



MATH 122

3.3: THE CHAIN RULE

PRODUCT AN QUOTIENT RULES

Differentiate e^{3x} .

- $f'(x) = e^x$.
- $g'(x) = \frac{d}{dx}(3x) = 3\frac{d}{dx}(x) = 3(1) = 3.$
- $f' \circ g(x) = f'(g(x)) = f'(3x) = e^{3x}$.
- Therefore by the Chain Rule

$$\frac{d}{dx} \left(e^{3x} \right) = \frac{d}{dx} \left(f \circ g(x) \right) = \left(f' \circ g(x) \right) \cdot g'(x)$$

$$= e^{3x} \cdot 3$$

$$= 3e^{3x}.$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AND QUOTIENT RULES

Differentiate $(\ln(2t^2+3))^2$.



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE
PRODUCT AN
QUOTIENT
RULES

Differentiate $(\ln(2t^2+3))^2$.

If we let
$$f(t) =$$
_ and $g(t) =$ _____, then $f \circ g(t) = \left(\ln\left(2t^2 + 3\right)\right)^2$.



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE
PRODUCT AN
QUOTIENT
RULES

Differentiate $(\ln(2t^2+3))^2$.

If we let
$$f(t) = \underline{t^2}$$
 and $g(t) = \underline{\ln(2t^2 + 3)}$, then $f \circ g(t) = \left(\ln(2t^2 + 3)\right)^2$.



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AND QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let
$$f(t) = \underline{t^2}$$
 and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$f\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

To differentiate g, we need to use the Chain Rule!



MATH 122

CLIFTON

3.3: THE CHAIN RULE

PRODUCT AN QUOTIENT RULES

Differentiate $\left(\ln\left(2t^2+3\right)\right)^2$.

If we let $f(t)=\underline{t^2}$ and $g(t)=\underline{\ln\left(2t^2+3\right)}$, then

If we let
$$I(t) = \underline{t}$$
 and $g(t) = \underline{\ln(2t^2 + 3)}$, then $f \circ g(t) = \left(\ln(2t^2 + 3)\right)^2$.

To differentiate g, we need to use the Chain Rule! If we let $h(t) = \underline{\hspace{1cm}}$ and $k(t) = \underline{\hspace{1cm}}$, then $h \circ k(t) = \underline{\hspace{1cm}}$

$$\left(\ln\left(2t^2+3\right)\right)^2.$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let
$$f(t) = \underline{t^2}$$
 and $g(t) = \underline{\ln(2t^2 + 3)}$, then $f \circ g(t) = (\ln(2t^2 + 3))^2$.



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let
$$f(t) = \underline{t^2}$$
 and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$f\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

To differentiate g, we need to use the Chain Rule! If we let $h(t) = \ln(t)$ and $k(t) = 2t^2 + 3$, then $h \circ k(t) = 2t^2 + 3$

$$\left(\ln\left(2t^2+3\right)\right)^2.$$

•
$$h'(t) = \frac{1}{t}$$
.



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$f\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

To differentiate g, we need to use the Chain Rule! If we let $h(t) = \frac{\ln(t)}{2}$ and $k(t) = \frac{2t^2 + 3}{2}$, then $h \circ k(t) = \frac{2t^2 + 3}{2}$

$$\left(\ln\left(2t^2+3\right)\right)^2.$$

$$\bullet h'(t) = \frac{1}{t}.$$

•
$$k'(t) =$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$f\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

To differentiate g, we need to use the Chain Rule! If we let $h(t) = \frac{\ln(t)}{2}$ and $k(t) = \frac{2t^2 + 3}{2}$, then $h \circ k(t) = \frac{2t^2 + 3}{2}$

$$\left(\ln\left(2t^2+3\right)\right)^2.$$

•
$$h'(t) = \frac{1}{t}$$
.

•
$$k'(t) = \frac{d}{dt}(2t^2 + 3) =$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$f\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

To differentiate g, we need to use the Chain Rule! If we let $h(t) = \frac{\ln(t)}{\ln(t)}$ and $k(t) = \frac{2t^2 + 3}{\ln(t)}$, then $h \circ k(t) = \frac{\ln(t)}{\ln(t)}$

$$\left(\ln\left(2t^2+3\right)\right)^2.$$

•
$$h'(t) = \frac{1}{t}$$
.

•
$$k'(t) = \frac{d}{dt}(2t^2 + 3) = \frac{d}{dt}(2t^2) + \frac{d}{dt}(3)) =$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let
$$f(t) = \underline{t^2}$$
 and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$\underline{f}\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

- - $k'(t) = \frac{d}{dt}(2t^2+3) = \frac{d}{dt}(2t^2) + \frac{d}{dt}(3)) = 2\frac{d}{dt}(t^2) + 0 = 0$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let
$$f(t) = \underline{t^2}$$
 and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$f\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

- $h'(t) = \frac{1}{t}$.
- $k'(t) = \frac{d}{dt}(2t^2+3) = \frac{d}{dt}(2t^2) + \frac{d}{dt}(3)) = 2\frac{d}{dt}(t^2) + 0 = 4t.$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$\underline{f}\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

- $h'(t) = \frac{1}{t}$.
- $k'(t) = \frac{d}{dt}(2t^2+3) = \frac{d}{dt}(2t^2) + \frac{d}{dt}(3)) = 2\frac{d}{dt}(t^2) + 0 = 4t.$
- $h' \circ k(t) =$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$f\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

- $h'(t) = \frac{1}{t}$.
- $k'(t) = \frac{d}{dt}(2t^2+3) = \frac{d}{dt}(2t^2) + \frac{d}{dt}(3)) = 2\frac{d}{dt}(t^2) + 0 = 4t.$
- $h' \circ k(t) = h'(k(t)) =$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let
$$f(t) = \underline{t^2}$$
 and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$f\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

- $h'(t) = \frac{1}{t}$.
- $k'(t) = \frac{d}{dt}(2t^2+3) = \frac{d}{dt}(2t^2) + \frac{d}{dt}(3)) = 2\frac{d}{dt}(t^2) + 0 = 4t.$
- $h' \circ k(t) = h'(k(t)) = h'(2t^2 + 3) =$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let
$$f(t) = \underline{t^2}$$
 and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$f\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

- $h'(t) = \frac{1}{t}$.
- $k'(t) = \frac{d}{dt}(2t^2+3) = \frac{d}{dt}(2t^2) + \frac{d}{dt}(3)) = 2\frac{d}{dt}(t^2) + 0 = 4t.$
- $h' \circ k(t) = h'(k(t)) = h'(2t^2 + 3) = \frac{1}{2t^2 + 3}$.



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then $f \circ g(t) = (\ln(2t^2 + 3))^2$.

- $h'(t) = \frac{1}{t}$.
- $k'(t) = \frac{d}{dt}(2t^2+3) = \frac{d}{dt}(2t^2) + \frac{d}{dt}(3)) = 2\frac{d}{dt}(t^2) + 0 = 4t.$
- $h' \circ k(t) = h'(k(t)) = h'(2t^2 + 3) = \frac{1}{2t^2 + 3}$.
- Therefore by the Chain Rule,

$$g'(t) = \frac{1}{2t^2 + 3} \cdot 4t = \frac{4t}{2t^2 + 3}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE Product an Quotient Rules Differentiate $(\ln(2t^2+3))^2$.

If we let
$$f(t) = \underline{t^2}$$
 and $g(t) = \underline{\ln(2t^2+3)}$, then $f \circ g(t) = \left(\ln(2t^2+3)\right)^2$. So we have:



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t)=\underline{t^2}$ and $g(t)=\underline{\ln\left(2t^2+3\right)}$, then $f\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2$. So we have:

$$g'(t) = \frac{4t}{2t^2+3}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then $f \circ g(t) = \left(\ln(2t^2 + 3)\right)^2$.

- $g'(t) = \frac{4t}{2t^2+3}$
- f'(t) = 2t



MATH 122

CLIFTON

3.3: THE CHAIN RULE

5.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then

$$f\circ g(t)=\left(\ln\left(2t^2+3\right)\right)^2.$$

- $g'(t) = \frac{4t}{2t^2+3}$
- f'(t) = 2t
- $f' \circ g(t) =$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then $f \circ g(t) = (\ln(2t^2 + 3))^2$.

- $g'(t) = \frac{4t}{2t^2+3}$
- f'(t) = 2t
- $f' \circ g(t) = f'(\ln(2t^2+3)) =$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2+3)}$, then $f \circ g(t) = \left(\ln(2t^2+3)\right)^2$.

$$\bullet g'(t) = \frac{4t}{2t^2+3}$$

•
$$f'(t) = 2t$$

•
$$f' \circ g(t) = f'(\ln(2t^2+3)) = 2\ln(2t^2+3)$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then $f \circ g(t) = \left(\ln(2t^2 + 3)\right)^2$. So we have:

- So we have.
 - $g'(t) = \frac{4t}{2t^2+3}$
 - f'(t) = 2t
 - $f' \circ g(t) = f'(\ln(2t^2+3)) = 2\ln(2t^2+3)$

$$\frac{d}{dt}\left(\ln\left(2t^2+3\right)\right)^2 =$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then $f \circ g(t) = \left(\ln(2t^2 + 3)\right)^2$.

$$g'(t) = \frac{4t}{2t^2+3}$$

•
$$f'(t) = 2t$$

•
$$f' \circ g(t) = f'(\ln(2t^2+3)) = 2\ln(2t^2+3)$$

$$\frac{\mathsf{d}}{\mathsf{d}t} \left(\mathsf{ln} \left(2t^2 + 3 \right) \right)^2 = (t' \circ g(t)) \cdot g'(t)$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then $f \circ g(t) = \left(\ln(2t^2 + 3)\right)^2$.

$$g'(t) = \frac{4t}{2t^2+3}$$

•
$$f'(t) = 2t$$

•
$$f' \circ g(t) = f'(\ln(2t^2 + 3)) = 2\ln(2t^2 + 3)$$

$$\frac{d}{dt} \left(\ln \left(2t^2 + 3 \right) \right)^2 = \left(f' \circ g(t) \right) \cdot g'(t)$$

$$= 2 \ln(2t^2 + 3) \cdot \frac{4t}{2t^2 + 3}$$

MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES Differentiate $(\ln(2t^2+3))^2$.

If we let $f(t) = \underline{t^2}$ and $g(t) = \underline{\ln(2t^2 + 3)}$, then $f \circ g(t) = (\ln(2t^2 + 3))^2$.

- $g'(t) = \frac{4t}{2t^2+3}$
- f'(t) = 2t
- $f' \circ g(t) = f'(\ln(2t^2 + 3)) = 2\ln(2t^2 + 3)$

$$\frac{d}{dt}\left(\ln\left(2t^2+3\right)\right)^2 = \left(f'\circ g(t)\right)\cdot g'(t)$$

$$= 2\ln(2t^2+3)\cdot \frac{4t}{2t^2+3}$$

$$= \frac{8t\ln(2t^2+3)}{2t^2+3}.$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

PRODUCT ANI
QUOTIENT
RULES

The last problem is a specific example of iterated use of the chain rule.



MATH 122

CLIFTON

3.3: THE CHAIN RULE

PRODUCT ANI
QUOTIENT
RULES

The last problem is a specific example of iterated use of the chain rule.



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

$$\frac{d}{dt}(f\circ (g\circ h)(t)) =$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

$$\frac{d}{dt}(f\circ(g\circ h)(t)) = (f'\circ(g\circ h)(t))\cdot\frac{d}{dt}(g\circ h(t))$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

$$\frac{d}{dt}(f\circ(g\circ h)(t)) = (f'\circ(g\circ h)(t))\cdot\frac{d}{dt}(g\circ h(t))$$
$$= (f'\circ(g\circ h)(t))\cdot(g'\circ h(t))\cdot h'(t)$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

$$\frac{d}{dt}(f \circ (g \circ h)(t)) = (f' \circ (g \circ h)(t)) \cdot \frac{d}{dt}(g \circ h(t))$$

$$= (f' \circ (g \circ h)(t)) \cdot (g' \circ h(t)) \cdot h'(t)$$

$$= f'(\ln(2t^2 + 3)) \cdot g'(2t^2 + 3) \cdot 4t$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

$$\frac{d}{dt}(f \circ (g \circ h)(t)) = (f' \circ (g \circ h)(t)) \cdot \frac{d}{dt}(g \circ h(t))$$

$$= (f' \circ (g \circ h)(t)) \cdot (g' \circ h(t)) \cdot h'(t)$$

$$= f'(\ln(2t^2 + 3)) \cdot g'(2t^2 + 3) \cdot 4t$$

$$= 2\ln(2t^2 + 3) \cdot \frac{1}{2t^2 + 3} \cdot 4t$$

MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

$$\frac{d}{dt}(f \circ (g \circ h)(t)) = (f' \circ (g \circ h)(t)) \cdot \frac{d}{dt}(g \circ h(t))
= (f' \circ (g \circ h)(t)) \cdot (g' \circ h(t)) \cdot h'(t)
= f'(\ln(2t^2 + 3)) \cdot g'(2t^2 + 3) \cdot 4t
= 2\ln(2t^2 + 3) \cdot \frac{1}{2t^2 + 3} \cdot 4t
= \frac{8t\ln(2t^2 + 3)}{2t^2 + 3}.$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

 The amount of gas, G, in gallons, consumed by a car depends on the distance, s, traveled in miles, which in turn depends on the time traveled, t.



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

- The amount of gas, G, in gallons, consumed by a car depends on the distance, s, traveled in miles, which in turn depends on the time traveled, t.
- If the car consumes 0.05 gallons for each mile traveled and the car is traveling 30 mph, then how fast is the gas being consumed?



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

- The amount of gas, G, in gallons, consumed by a car depends on the distance, s, traveled in miles, which in turn depends on the time traveled, t.
- If the car consumes 0.05 gallons for each mile traveled and the car is traveling 30 mph, then how fast is the gas being consumed?

•

$$\frac{\mathsf{d}}{\mathsf{d}t}(G\circ s(t))$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

- The amount of gas, G, in gallons, consumed by a car depends on the distance, s, traveled in miles, which in turn depends on the time traveled, t.
- If the car consumes 0.05 gallons for each mile traveled and the car is traveling 30 mph, then how fast is the gas being consumed?

•

$$\frac{\mathsf{d}}{\mathsf{d}\mathsf{t}}(G\circ s(t)) = (G'\circ s(t))\cdot s'(t)$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

- The amount of gas, G, in gallons, consumed by a car depends on the distance, s, traveled in miles, which in turn depends on the time traveled, t.
- If the car consumes 0.05 gallons for each mile traveled and the car is traveling 30 mph, then how fast is the gas being consumed?

6

$$\frac{d}{dt}(G \circ s(t)) = (G' \circ s(t)) \cdot s'(t)$$

$$= 0.05 \frac{gal}{mile} \cdot 30 \frac{miles}{hour}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

- The amount of gas, G, in gallons, consumed by a car depends on the distance, s, traveled in miles, which in turn depends on the time traveled, t.
- If the car consumes 0.05 gallons for each mile traveled and the car is traveling 30 mph, then how fast is the gas being consumed?

4

$$\frac{d}{dt}(G \circ s(t)) = (G' \circ s(t)) \cdot s'(t)$$

$$= 0.05 \frac{gal}{mile} \cdot 30 \frac{miles}{hour}$$

$$= 1.5 \frac{gal}{hour}.$$



PRODUCT RULE

MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

If f and g are differentiable functions, then

$$\frac{\mathrm{d}}{\mathrm{d}x}(f(x)g(x))=f'(x)g(x)+f(x)g'(x).$$



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

Assume that f and g are differentiable functions and f(x)/g(x) is well-defined.



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AND QUOTIENT RULES



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AN QUOTIENT RULES

$$\frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) = \frac{d}{dx}\left(f(x)g(x)^{-1}\right)$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AND QUOTIENT RULES

$$\frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) = \frac{d}{dx}\left(f(x)g(x)^{-1}\right)$$
$$= f'(x)g(x)^{-1} + f(x)\frac{d}{dx}\left(g(x)^{-1}\right)$$



MATH 122

3.3: THE

3.4: THE PRODUCT AND QUOTIENT RULES

$$\frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) = \frac{d}{dx}\left(f(x)g(x)^{-1}\right)$$

$$= f'(x)g(x)^{-1} + f(x)\frac{d}{dx}\left(g(x)^{-1}\right)$$

$$= \frac{f'(x)}{g(x)} + f(x)\left((-1)g(x)^{-2}g'(x)\right)$$



MATH 122

3.3: THE

3.4: THE PRODUCT AN QUOTIENT RULES

$$\frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) = \frac{d}{dx}\left(f(x)g(x)^{-1}\right)$$

$$= f'(x)g(x)^{-1} + f(x)\frac{d}{dx}\left(g(x)^{-1}\right)$$

$$= \frac{f'(x)}{g(x)} + f(x)\left((-1)g(x)^{-2}g'(x)\right)$$

$$= \frac{f'(x)}{g(x)} - \frac{f(x)g'(x)}{g(x)^{2}}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AND QUOTIENT RULES

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{d}{dx} \left(f(x)g(x)^{-1} \right)
= f'(x)g(x)^{-1} + f(x)\frac{d}{dx} \left(g(x)^{-1} \right)
= \frac{f'(x)}{g(x)} + f(x) \left((-1)g(x)^{-2}g'(x) \right)
= \frac{f'(x)}{g(x)} - \frac{f(x)g'(x)}{g(x)^2}
= \frac{f'(x)g(x) - f(x)g'(x)}{g(x)^2}.$$

MATH 122

CLIFTO

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

Differentiate

(A)
$$x^2e^{2x}$$

(B)
$$t^3 \ln(t+1)$$

(c)
$$(3x^2 + 5x)e^x$$



MATH 122

3.4: THE PRODUCT AND QUOTIENT RULES

Differentiate

(A)
$$x^2e^{2x}$$

(B)
$$t^3 \ln(t+1)$$

(B)
$$t^3 \ln(t+1)$$
 (C) $(3x^2+5x)e^x$

$$\frac{\mathrm{d}}{\mathrm{d}x}(x^2e^{2x}) =$$



MATH 122

3.4: THE PRODUCT AND QUOTIENT RULES

Differentiate

(A)
$$x^2e^{2x}$$

(B)
$$t^3 \ln(t+1)$$

(B)
$$t^3 \ln(t+1)$$
 (C) $(3x^2+5x)e^x$

$$\frac{d}{dx}(x^2e^{2x}) = \frac{d}{dx}(x^2) \cdot e^{2x} + x^2 \cdot \frac{d}{dx}(e^{2x})$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$x^2e^{2x}$$
 (B) $t^3\ln(t+1)$ (C) $(3x^2+5x)e^x$

$$\frac{d}{dx}(x^2e^{2x}) = \frac{d}{dx}(x^2) \cdot e^{2x} + x^2 \cdot \frac{d}{dx}(e^{2x})$$
$$= 2xe^{2x} + x^2 \left(\frac{d}{dx}(2x) \cdot e^{2x}\right)$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$x^2e^{2x}$$
 (B) $t^3\ln(t+1)$ (C) $(3x^2+5x)e^x$

$$\frac{d}{dx}(x^2e^{2x}) = \frac{d}{dx}(x^2) \cdot e^{2x} + x^2 \cdot \frac{d}{dx}(e^{2x})$$
$$= 2xe^{2x} + x^2 \left(\frac{d}{dx}(2x) \cdot e^{2x}\right)$$
$$= 2xe^{2x} + 2x^2e^{2x}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$x^2e^{2x}$$
 (B) $t^3\ln(t+1)$ (C) $(3x^2+5x)e^x$

$$\frac{d}{dx}(x^{2}e^{2x}) = \frac{d}{dx}(x^{2}) \cdot e^{2x} + x^{2} \cdot \frac{d}{dx}(e^{2x})$$

$$= 2xe^{2x} + x^{2}\left(\frac{d}{dx}(2x) \cdot e^{2x}\right)$$

$$= 2xe^{2x} + 2x^{2}e^{2x}$$

$$= 2xe^{2x}(1+x)$$



MATH 122

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$x^2e^{2x}$$

(B)
$$t^3 \ln(t+1)$$

(B)
$$t^3 \ln(t+1)$$
 (C) $(3x^2 + 5x)e^x$

$$\frac{\mathrm{d}}{\mathrm{d}t}(t^3\ln(t+1))$$



MATH 122

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$x^2e^{2x}$$

(B)
$$t^3 \ln(t+1)$$

(B)
$$t^3 \ln(t+1)$$
 (C) $(3x^2 + 5x)e^x$

$$\frac{\mathrm{d}}{\mathrm{d}t}(t^3\ln(t+1)) = \frac{\mathrm{d}}{\mathrm{d}t}(t^3)\cdot\ln(t+1)+t^3\cdot\frac{\mathrm{d}}{\mathrm{d}t}\left(\ln(t+1)\right)$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$x^2e^{2x}$$
 (B) $t^3\ln(t+1)$ (C) $(3x^2+5x)e^x$

$$\frac{d}{dt}(t^3 \ln(t+1)) = \frac{d}{dt}(t^3) \cdot \ln(t+1) + t^3 \cdot \frac{d}{dt}(\ln(t+1))$$
$$= 3t^2 \ln(t+1) + t^3 \left(\frac{\frac{d}{dt}(t+1)}{t+1}\right)$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$x^2e^{2x}$$
 (B) $t^3\ln(t+1)$ (C) $(3x^2+5x)e^x$

$$\frac{d}{dt}(t^3 \ln(t+1)) = \frac{d}{dt}(t^3) \cdot \ln(t+1) + t^3 \cdot \frac{d}{dt}(\ln(t+1))$$

$$= 3t^2 \ln(t+1) + t^3 \left(\frac{\frac{d}{dt}(t+1)}{t+1}\right)$$

$$= 3t^2 \ln(t+1) + \frac{t^3}{t+1}.$$

MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$x^2 e^{2x}$$

(B)
$$t^3 \ln(t+1)$$

(C)
$$(3x^2 + 5x)e^x$$

$$\frac{d}{dx}\left((3x^2+5x)e^x\right) =$$

MATH 122

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$x^2 e^{2x}$$

(B)
$$t^3 \ln(t+1)$$

(B)
$$t^3 \ln(t+1)$$
 (C) $(3x^2 + 5x)e^x$

$$\frac{d}{dx}\left((3x^2+5x)e^x\right) = \frac{d}{dx}(3x^2+5x)\cdot e^x + (3x^2+5x)\cdot \frac{d}{de^x}$$

MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$x^2e^{2x}$$

(B)
$$t^3 \ln(t+1)$$

(C)
$$(3x^2 + 5x)e^x$$

$$\frac{d}{dx} \left((3x^2 + 5x)e^x \right) = \frac{d}{dx} (3x^2 + 5x) \cdot e^x + (3x^2 + 5x) \cdot \frac{d}{de^x}$$
$$= (6x + 5)e^x + (3x^2 + 5x)e^x$$

MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

Differentiate

(A)
$$x^2e^{2x}$$

$$\frac{d}{dx} \left((3x^2 + 5x)e^x \right) = \frac{d}{dx} (3x^2 + 5x) \cdot e^x + (3x^2 + 5x) \cdot \frac{d}{de^x}
= (6x + 5)e^x + (3x^2 + 5x)e^x
= e^x (6x + 5 + 3x^2 + 5x)$$

(B) $t^3 \ln(t+1)$

(c) $(3x^2 + 5x)e^x$

MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$x^2e^{2x}$$

(B)
$$t^3 \ln(t+1)$$

(C)
$$(3x^2 + 5x)e^x$$

$$\frac{d}{dx}\left((3x^2+5x)e^x\right) = \frac{d}{dx}(3x^2+5x) \cdot e^x + (3x^2+5x) \cdot \frac{d}{de^x}$$

$$= (6x+5)e^x + (3x^2+5x)e^x$$

$$= e^x(6x+5+3x^2+5x)$$

$$= e^x(3x^2+11x+5).$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

$$\frac{\mathrm{d}}{\mathrm{d}t}\frac{e^{2t}}{t}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULL

3.4: THE PRODUCT AND QUOTIENT RULES

$$\frac{\mathrm{d}}{\mathrm{d}t}\frac{\mathrm{e}^{2t}}{t} \ = \ \frac{\frac{\mathrm{d}}{\mathrm{d}t}\left(\mathrm{e}^{2t}\right)\cdot t - \mathrm{e}^{2t}\cdot\frac{\mathrm{d}}{\mathrm{d}t}(t)}{t^2}$$



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

$$\begin{array}{ll} \frac{\mathrm{d}}{\mathrm{d}t} \frac{\mathrm{e}^{2t}}{t} & = & \frac{\frac{\mathrm{d}}{\mathrm{d}t} \left(\mathrm{e}^{2t}\right) \cdot t - \mathrm{e}^{2t} \cdot \frac{\mathrm{d}}{\mathrm{d}t}(t)}{t^2} \\ & = & \frac{\frac{\mathrm{d}}{\mathrm{d}t} (2t) \cdot t \mathrm{e}^{2t} - \mathrm{e}^{2t}(1)}{t^2} \end{array}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

$$\frac{d}{dt} \frac{e^{2t}}{t} = \frac{\frac{d}{dt} \left(e^{2t}\right) \cdot t - e^{2t} \cdot \frac{d}{dt}(t)}{t^2}$$

$$= \frac{\frac{d}{dt} (2t) \cdot t e^{2t} - e^{2t}(1)}{t^2}$$

$$= \frac{2te^{2t} - e^{2t}}{t^2}$$



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

$$\frac{d}{dt} \frac{e^{2t}}{t} = \frac{\frac{d}{dt} (e^{2t}) \cdot t - e^{2t} \cdot \frac{d}{dt} (t)}{t^2}$$

$$= \frac{\frac{d}{dt} (2t) \cdot t e^{2t} - e^{2t} (1)}{t^2}$$

$$= \frac{2t e^{2t} - e^{2t}}{t^2}$$

$$= \frac{(2t - 1)e^{2t}}{t^2}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

A product's price, *p*, is given by

$$p(q) = 80e^{-0.003q},$$



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES A product's price, p, is given by

$$p(q) = 80e^{-0.003q},$$

where q is the quantity sold.

(A) Find the revenue as a function of the quantity sold.



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES A product's price, *p*, is given by

$$p(q) = 80e^{-0.003q},$$

- (A) Find the revenue as a function of the quantity sold.
- (B) How does revenue vary with respect to quantity?



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES A product's price, p, is given by

$$p(q) = 80e^{-0.003q},$$

- (A) Find the revenue as a function of the quantity sold.
- (B) How does revenue vary with respect to quantity?

$$R(q) = p(q) \cdot q$$



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES A product's price, p, is given by

$$p(q) = 80e^{-0.003q},$$

- (A) Find the revenue as a function of the quantity sold.
- (B) How does revenue vary with respect to quantity?

$$R(q) = p(q) \cdot q = 80e^{-0.003q}q$$



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES A product's price, p, is given by

$$p(q) = 80e^{-0.003q},$$

- (A) Find the revenue as a function of the quantity sold.
- (B) How does revenue vary with respect to quantity?

$$R(q) = p(q) \cdot q = 80e^{-0.003q}q = 80qe^{-0.003q}$$
.



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES A product's price, p, is given by

$$p(q) = 80e^{-0.003q},$$

- (A) Find the revenue as a function of the quantity sold.
- (B) How does revenue vary with respect to quantity?

$$R(q) = p(q) \cdot q = 80e^{-0.003q}q = 80qe^{-0.003q}$$
.

$$\frac{d}{dq}R(q) = \frac{d}{dq}(80qe^{-0.003q})$$



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AN QUOTIENT RULES A product's price, p, is given by

$$p(q) = 80e^{-0.003q},$$

- (A) Find the revenue as a function of the quantity sold.
- (B) How does revenue vary with respect to quantity?

$$R(q) = p(q) \cdot q = 80e^{-0.003q}q = 80qe^{-0.003q}$$

$$\frac{d}{dq}R(q) = \frac{d}{dq}(80qe^{-0.003q})$$
$$= 80\frac{d}{dq}qe^{-0.003q}$$



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AN QUOTIENT RULES A product's price, p, is given by

$$p(q) = 80e^{-0.003q},$$

- (A) Find the revenue as a function of the quantity sold.
- (B) How does revenue vary with respect to quantity?

$$R(q) = p(q) \cdot q = 80e^{-0.003q}q = 80qe^{-0.003q}$$

$$\frac{d}{dq}R(q) = \frac{d}{dq}(80qe^{-0.003q})$$

$$= 80\frac{d}{dq}qe^{-0.003q}$$

$$= 80(e^{-0.003q} + q(-0.003)e^{-0.003q})$$



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AN QUOTIENT RULES A product's price, *p*, is given by

$$p(q) = 80e^{-0.003q},$$

- (A) Find the revenue as a function of the quantity sold.
- (B) How does revenue vary with respect to quantity?

$$R(q) = p(q) \cdot q = 80e^{-0.003q}q = 80qe^{-0.003q}$$
.

$$\frac{d}{dq}R(q) = \frac{d}{dq}(80qe^{-0.003q})$$

$$= 80\frac{d}{dq}qe^{-0.003q}$$

$$= 80(e^{-0.003q} + q(-0.003)e^{-0.003q})$$

$$= 80e^{-0.003q}(1 - 0.003q).$$

MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$

(B)
$$\frac{1}{1 + e^x}$$

(C)
$$\frac{e^{x}}{x^2}$$
.

MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$

(B)
$$\frac{1}{1+e^x}$$

(C)
$$\frac{e^x}{x^2}$$

$$\frac{\mathsf{d}}{\mathsf{d}x}\left(\frac{5x^2}{x^3+1}\right)$$

MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$

(B)
$$\frac{1}{1 + e^x}$$
 (C) $\frac{e^x}{x^2}$.

$$\frac{d}{dx}\left(\frac{5x^2}{x^3+1}\right) = \frac{10x(x^3+1)-5x^2(3x^2)}{(x^3+1)^2}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$
 (B) $\frac{1}{1+e^x}$ (C) $\frac{e^x}{x^2}$.

$$\frac{d}{dx}\left(\frac{5x^2}{x^3+1}\right) = \frac{10x(x^3+1)-5x^2(3x^2)}{(x^3+1)^2}$$
$$= \frac{10x^4+10x-15x^4}{(x^3+1)^2}$$

MATH 122

CLIFTON

3.3: THE CHAIN RULE

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$
 (B) $\frac{1}{1+e^x}$ (C) $\frac{e^x}{x^2}$.

$$\frac{d}{dx}\left(\frac{5x^2}{x^3+1}\right) = \frac{10x(x^3+1)-5x^2(3x^2)}{(x^3+1)^2}$$

$$= \frac{10x^4+10x-15x^4}{(x^3+1)^2}$$

$$= \frac{-5x^4+10}{(x^3+1)^2}.$$

MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$

(B)
$$\frac{1}{1+e^x}$$

(C)
$$\frac{e^x}{x^2}$$
.

$$\frac{\mathrm{d}}{\mathrm{d}x}\frac{1}{1+e^{x}}$$

MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$

(B)
$$\frac{1}{1+e^x}$$

(C)
$$\frac{e^x}{x^2}$$
.

$$\frac{d}{dx}\frac{1}{1+e^x} = \frac{0(1+e^x)-(1)e^x}{(1+e^x)^2}$$

MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$

(B)
$$\frac{1}{1+e^{x}}$$

(C)
$$\frac{e^x}{x^2}$$
.

$$\frac{d}{dx}\frac{1}{1+e^x} = \frac{0(1+e^x)-(1)e^x}{(1+e^x)^2}$$
$$= \frac{-e^x}{(1+e^x)^2}.$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$

(B)
$$\frac{1}{1+e^x}$$

(C)
$$\frac{e^x}{x^2}$$
.

$$\frac{d}{dx}\frac{e^{x}}{x^{2}}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$

(B)
$$\frac{1}{1+e^x}$$

C)
$$\frac{e^x}{v^2}$$
.

$$\frac{\mathrm{d}}{\mathrm{d}x}\frac{e^x}{x^2} = \frac{e^x x^2 - e^x (2x)}{x^4}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$

(B)
$$\frac{1}{1 + e^x}$$
 (C) $\frac{e^x}{x^2}$

$$\frac{d}{dx}\frac{e^x}{x^2} = \frac{e^x x^2 - e^x(2x)}{x^4}$$
$$= \frac{e^x (x^2 - 2x)}{x^4}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$

(B)
$$\frac{1}{1 + e^x}$$
 (C) $\frac{e^x}{x^2}$

$$\frac{d}{dx}\frac{e^x}{x^2} = \frac{e^x x^2 - e^x (2x)}{x^4}$$
$$= \frac{e^x (x^2 - 2x)}{x^4}$$
$$= \frac{e^x (x)(x - 2)}{x^4}$$



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

(A)
$$\frac{5x^2}{x^3+1}$$

(B)
$$\frac{1}{1 + e^x}$$
 (C) $\frac{e^x}{x^2}$

$$\frac{d}{dx}\frac{e^x}{x^2} = \frac{e^x x^2 - e^x (2x)}{x^4}$$

$$= \frac{e^x (x^2 - 2x)}{x^4}$$

$$= \frac{e^x (x)(x - 2)}{x^4}$$

$$= \frac{e^x (x - 2)}{x^3}.$$



MATH 122

CLIFTO

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$f'(2) = 5$$
,

MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$f'(2) = 5$$
,

•
$$g(2) = 3$$
,

MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$f'(2) = 5$$
,

•
$$g(2) = 3$$
,

•
$$g'(2) = 6$$
.

MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$f'(2) = 5$$
,

•
$$g(2) = 3$$
,

•
$$g'(2) = 6$$
.

Let
$$h(x) = f(x)g(x)$$
 and $k(x) = f(x)/g(x)$. Find

MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$f'(2) = 5$$
,

•
$$g(2) = 3$$
,

•
$$g'(2) = 6$$
.

Let
$$h(x) = f(x)g(x)$$
 and $k(x) = f(x)/g(x)$. Find

(A)
$$h'(2)$$
,

MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$f'(2) = 5$$
,

•
$$g(2) = 3$$
,

•
$$g'(2) = 6$$
.

Let
$$h(x) = f(x)g(x)$$
 and $k(x) = f(x)/g(x)$. Find

(A)
$$h'(2)$$
,

(B)
$$k'(2)$$
.



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$g(2) = 3$$
,

•
$$f'(2) = 5$$
,

•
$$g'(2) = 6$$
.

Let
$$h(x) = f(x)g(x)$$
 and $k(x) = f(x)/g(x)$. Find

(A)
$$h'(2)$$
,

(B)
$$k'(2)$$
.

$$h'(2) =$$



MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$g(2) = 3$$
,

•
$$f'(2) = 5$$
,

•
$$g'(2) = 6$$
.

Let
$$h(x) = f(x)g(x)$$
 and $k(x) = f(x)/g(x)$. Find

(A)
$$h'(2)$$
,

(B)
$$k'(2)$$
.

$$h'(2) = f'(2)g(2) + f(2)g'(2)$$

MATH 122

CLIFION

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$g(2) = 3$$
,

•
$$f'(2) = 5$$
,

•
$$g'(2) = 6$$
.

Let
$$h(x) = f(x)g(x)$$
 and $k(x) = f(x)/g(x)$. Find

(A)
$$h'(2)$$
,

(B)
$$k'(2)$$
.

$$h'(2) = f'(2)g(2) + f(2)g'(2)$$

= 5(3) + 1(6)

MATH 122

CLIFTON

3.3: THE CHAIN RUL

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$g(2) = 3$$
,

•
$$f'(2) = 5$$
,

•
$$g'(2) = 6$$
.

Let
$$h(x) = f(x)g(x)$$
 and $k(x) = f(x)/g(x)$. Find

(A)
$$h'(2)$$
,

(B)
$$k'(2)$$
.

$$h'(2) = f'(2)g(2) + f(2)g'(2)$$

= 5(3) + 1(6)
= 21.



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$f'(2) = 5$$
,

•
$$g(2) = 3$$
,

•
$$g'(2) = 6$$
.

Let
$$h(x) = f(x)g(x)$$
 and $k(x) = f(x)/g(x)$. Find

(A)
$$h'(2)$$
,

(B)
$$k'(2)$$
.

$$k'(2) =$$



MATH 122

CLIFTON

3.3: The Chain Ruli

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$g(2) = 3$$
,

•
$$f'(2) = 5$$
,

•
$$g'(2) = 6$$
.

Let
$$h(x) = f(x)g(x)$$
 and $k(x) = f(x)/g(x)$. Find

(A)
$$h'(2)$$
,

(B)
$$k'(2)$$
.

$$k'(2) = \frac{f'(2)g(2) - f(2)g'(2)}{g(2)^2}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

•
$$f(2) = 1$$
,

•
$$g(2) = 3$$
,

•
$$f'(2) = 5$$
,

•
$$g'(2) = 6$$
.

Let
$$h(x) = f(x)g(x)$$
 and $k(x) = f(x)/g(x)$. Find

(A)
$$h'(2)$$
,

(B)
$$k'(2)$$
.

$$k'(2) = \frac{f'(2)g(2) - f(2)g'(2)}{g(2)^2}$$
$$= \frac{5(3) - 1(6)}{3^2}$$



MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

Assume

•
$$f(2) = 1$$
,

•
$$g(2) = 3$$
,

•
$$f'(2) = 5$$
,

•
$$g'(2) = 6$$
.

Let h(x) = f(x)g(x) and k(x) = f(x)/g(x). Find

(A)
$$h'(2)$$
,

(B) k'(2).

$$k'(2) = \frac{f'(2)g(2) - f(2)g'(2)}{g(2)^2}$$
$$= \frac{5(3) - 1(6)}{3^2}$$
$$= \frac{15 - 6}{9}$$

MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

Assume

•
$$f(2) = 1$$
,

•
$$g(2) = 3$$
,

•
$$f'(2) = 5$$
,

•
$$g'(2) = 6$$
.

Let h(x) = f(x)g(x) and k(x) = f(x)/g(x). Find

(A)
$$h'(2)$$
,

(B) k'(2).

$$k'(2) = \frac{f'(2)g(2) - f(2)g'(2)}{g(2)^2}$$
$$= \frac{5(3) - 1(6)}{3^2}$$
$$= \frac{15 - 6}{9} = \frac{9}{9}$$

MATH 122

CLIFTON

3.3: THE CHAIN RULI

3.4: THE PRODUCT AND QUOTIENT RULES

Assume

•
$$f(2) = 1$$
,

•
$$g(2) = 3$$
,

•
$$f'(2) = 5$$
,

•
$$g'(2) = 6$$
.

Let h(x) = f(x)g(x) and k(x) = f(x)/g(x). Find

(A)
$$h'(2)$$
,

(B) k'(2).

$$k'(2) = \frac{f'(2)g(2) - f(2)g'(2)}{g(2)^2}$$
$$= \frac{5(3) - 1(6)}{3^2}$$
$$= \frac{15 - 6}{9} = \frac{9}{9} = 1.$$