

**Homework 7 - Math 574, Frank Thorne (thornef@mailbox.sc.edu)**

**Due Monday, March 19 at 5:00.**

All homework turned in on time will be returned on Tuesday.

**Core:**

6.1: 3, 7, 10, 11, 13, 24, 33 (a, b).

For each integer  $i$ , let  $A_i = (i, i + 1)$  and let  $B_i = [i, i + 1]$ . Describe the sets  $\cup_{i \in \mathbb{Z}} A_i$  and  $\cup_{i \in \mathbb{Z}} B_i$ .

6.2: 7, 9, 13.

7.2: 5, 6, 9, 17, 18.

**Additional:**

6.1: 8, 12.

6.2: 8, 10, 14.

7.2: 10, 11, 15, 16.

**Bonus:**

(1) (2 points) 7.4: 14.

(2) (2 points) Find sets  $A_i$ , for each integer  $i \geq 1$ , such that  $\cap_{i \geq 1} A_i = \mathbb{Z}$ .

(3) (1,000,000 points) Is there a polynomial  $f(x, y)$  in two variables such that  $f$  gives a bijection from  $\mathbb{Q} \times \mathbb{Q}$  to  $\mathbb{Q}$ ?

*(Mheh heh heh. Good luck.)*