

Chapter 1
Section 1.1

Warm-up Problem A. Decide whether each of the following is an expression or an equation. How did you decide?

(a) $2(3t - 8) - 7t$

expression

(b) $-3x + 2 - 4 - x = 4 + 2x - 9$

equation

Warm-up Problem B. Decide whether the given value for the variable is a solution for the equation. How did you decide?

(a) $3d - 5 = 5(d - 3); d = -1$

*NO
plug & chug*

(b) $3|x + 4| = 5x; x = 6$

*yes
plug & chug*

Problem 1. Which equations are linear equations in x ?

(a) $x^2 + 3x = 5$

no

(b) $3x - 2 + x = 0$

yes

(c) $2(3x - 8) = 7$

yes

(d) $3x + \frac{8}{x} = -22$

no

Problem 2. Solve each equation. Decide whether there is one solution, infinitely many solutions, or no solutions. If there is one solution, check the solution.

(a) $11x - 14x - 7 + 8 = 4x + 5 - 2$

$-3x + 1 = 4x + 3$

$-\frac{2}{7} = x$

1 solution

(c) $4(k - 9) = 4(k + 3) - 48$

$4k - 24 = 4k - 36$

$0 = -12$

no solution

$\begin{array}{r} 48 \\ -12 \\ \hline 36 \\ -24 \\ \hline 12 \end{array}$

*absolute value doesn't fit this scheme
maybe make those their own problem...*

(b) $-6x + 2x - 11 = -2(2x - 3) + 4$

$-4x - 11 = -4x + 10$

$-11 = 10$

no sol'n

(d) $-9y - (5 + y) = -(3y - 1) - 6$

$-10y - 5 = -3y - 5$

$y = 0$

1-sol'n

$$(e) \frac{2m-1}{3} - \frac{3m}{4} = \frac{5}{6}$$

$$8m-4-9m=10$$

$$-m-4=10$$

$$m=-14$$

-1 sol'n

$$(f) \frac{1}{3n} - \frac{1}{4n} = \frac{1}{6}$$

$$4-3=2n$$

$$n=\frac{1}{2}$$

1 sol'n

$$(g) \frac{1}{n} + \frac{1}{n-3} = \frac{9}{n^2-3n}$$

$$n-3+n=9$$

$$2n=12$$

$$n=\frac{12}{2}$$

$n(n-3)$

1 sol'n

$$(h) \frac{5-12x}{3} - 3x + 11x = \frac{14x-6}{2} + \frac{5}{3}$$

$$10-24x-18x+66x=42x-18+10$$

$$10+24x=42x-8$$

$$\frac{-24x}{14x}$$

$$x=1 \quad 1 \text{ sol'n}$$

$$(i) 0.02(x+4) = 0.03x - 0.02$$

$$2x+8=3x-2$$

$$x=10$$

1 sol'n

$$(j) |2x| = 4$$

$$x = \pm 2$$

?

make its own section?

$$(k) |2x-3| = 4$$

$$2x-3=4 \rightarrow x=6$$

$$2x-3=-4 \rightarrow x=-\frac{1}{2}$$

$$(l) |2x-3| = 4+x$$

$$2x-3=-4-x \rightarrow x=-\frac{1}{3}$$

$$2x-3=4+x \rightarrow x=7$$

Additional Problems

EP 1. Solve each equation. Decide whether there is one solution, infinitely many solutions, or no solutions. If there is one solution, check the solution.

(a) $4(2x + 7) = 2x + 25 + 3(2x + 1)$

$$8x + 28 = 2x + 25 + 6x + 3$$

$$8x + 28 = 8x + 28$$

infinite
solutions

(b) $\frac{3}{11}x = -2$

$$x = \frac{-22}{3}$$

1-solution

(c) $2(-(t - 1) + 4) = 5 + (-(6t - 7) + 9t)$

$$-2t + 2 + 8 = 5 - 6t + 7 + 9t$$

$$-2t + 10 = 12 + 3t$$

$$t = 2 \quad 1\text{-sol'n}$$

(d) $\frac{8x}{3} - \frac{x}{2} = 4$

$$16x - 3x = 24$$

$$x = \frac{24}{13}$$

1-sol'n

(e) $\frac{2x+5}{5} = \frac{3x+1}{2} + \frac{-x+8}{16}$

$$32x + 40 = 120x + 40 - 5x + 40$$

$$83x = -40$$

$$x = \frac{-40}{83}$$

1-sol'n

(f) $0.05x + 0.08 + 0.06x = 0.07x + 0.68$

$$5x + 8 + 6x = 7x + 68$$

$$11x + 8 = 7x + 68$$

$$3x = 60$$

$$x = 20 \quad 1\text{-sol'n}$$

(g) $6(3 - 4x) + 10 = -15x + 3(2 - 3x)$

$$18 - 24x + 10 = -15x + 6 - 9x$$

$$-24x + 18 = -24x + 6$$

$$18 = 6$$

no sol'n