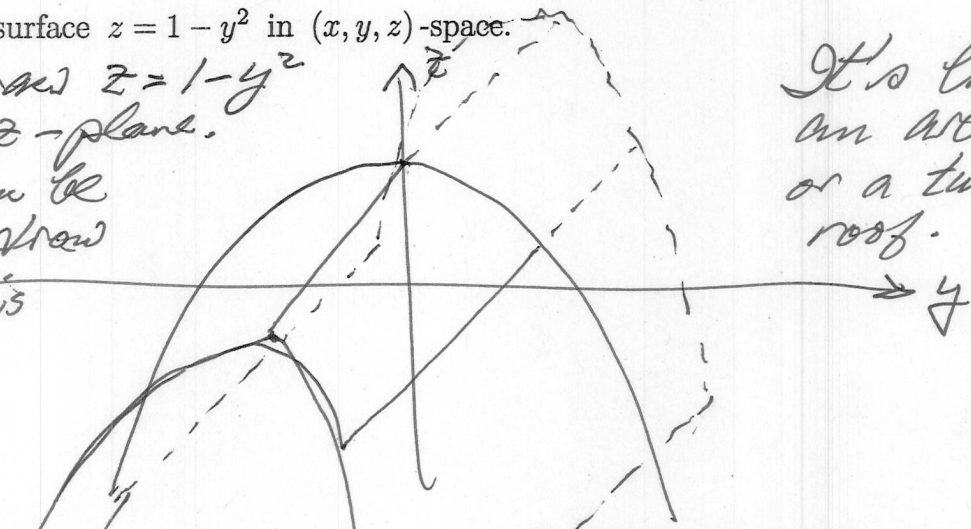


1. Sketch the surface  $z = 1 - y^2$  in  $(x, y, z)$ -space.

First draw  $z = 1 - y^2$   
in the  $yz$ -plane.  
Then  $x$  can be  
anything so draw  
lines  $\parallel$   $x$ -axis

It's like  
an arch  
or a tunnel  
roof.



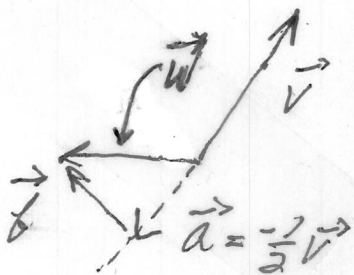
2. Find the terminal point  $Q$  of  $\mathbf{v} = \langle 1, 2, -3 \rangle = \hat{i} + 2\hat{j} - 3\hat{k}$  if the initial point  $P$  is  $(-2, 1, 4)$ . Also find the length of  $\mathbf{v}$ .

$Q$  is the point  $(-2+1, 1+2, 4-3)$   
 $= (-1, 3, 1)$

$$\|\mathbf{v}\| = \sqrt{1^2 + 2^2 + (-3)^2} = \sqrt{14}$$

3. Compute the orthogonal projection of  $\mathbf{w} = \langle 1, -1, 2 \rangle$  on  $\mathbf{v} = \langle 1, 2, -3 \rangle$  (that is,  $\mathbf{a} = \text{proj}_{\mathbf{v}} \mathbf{w}$ , the component of  $\mathbf{w}$  in the direction of  $\mathbf{v}$ ). Then compute the component of  $\mathbf{w}$  that is orthogonal to  $\mathbf{v}$ ; call this vector  $\mathbf{b}$ . Finally, verify that  $\mathbf{a}$  is orthogonal to  $\mathbf{b}$ .

$$\begin{aligned} \vec{a} &= \left( \frac{\vec{w} \cdot \vec{v}}{\vec{v} \cdot \vec{v}} \right) \vec{v} = \frac{1-2-6}{14} \langle 1, 2, -3 \rangle \\ &= -\frac{1}{2} \langle 1, 2, -3 \rangle = \left\langle -\frac{1}{2}, -1, \frac{3}{2} \right\rangle \end{aligned}$$



$$\begin{aligned} \vec{b} &= \vec{w} - \vec{a} \\ &= \left\langle \frac{3}{2}, 0, \frac{1}{2} \right\rangle \end{aligned}$$

$$\begin{aligned} \vec{a} \cdot \vec{b} &= \left(-\frac{1}{2}\right)\left(\frac{3}{2}\right) + 0 + \frac{3}{2}\left(\frac{1}{2}\right) \\ &= 0 \end{aligned}$$

so  $\vec{a} \perp \vec{b}$