

**MATH 122 Spring, 2004 Exam #1 Name: \_\_\_\_\_**

There are 100 points. For full credit you must show your work.

1. (15 points) Assuming  $L$  is a linear function of  $t$ , fill in the missing values in the table and find a formula for  $L$  as a function of  $t$ .

$t$		-1	0	1		4
$L$	10	6		2	0	-4

2. (15 points) There were 56,050 cars imported to the U.S. from Japan in 1966, and the number of Japanese imports grew at a discrete rate of 72% a year until 1972.
- a. How many Japanese cars were imported in 1968?
- b. Give a formula for the number of Japanese imports,  $N(t)$ , where  $t$  is measured in years since 1966. How many cars were imported in 1965?

3. (15 points) A company that makes overpriced retro style blenders has fixed costs of \$16,800 and variable costs of \$45 per machine. The company plans to sell the machines for \$125 each. Let  $q$  represent the number of blenders. Give formulas for the cost function  $C(q)$  and the revenue function  $R(q)$ . What is the break-even point in terms of number of blenders?

4. (10 points) The graph of a certain function  $f$  is shown below.
- This graph shows \_\_\_\_\_ as a function of \_\_\_\_\_ .
  - Compute the average rate of change from  $x = 4$  to  $x = 9$ , and illustrate the geometric meaning of this computation.

b. For which values of  $x$  is the graph concave up?

5. (15 points) When X-rays pass through a heavy concrete shield the intensity of the radiation  $R$  decreases exponentially; that is,  $R = R_0 e^{kx}$ . The initial amount is  $R_0$ , the thickness of the concrete is  $x$ , and the “decay” rate is  $k$ . It takes 3 feet of concrete to remove 75% of the X-ray radiation (so 25% remains).
- Determine the decay rate  $k$ .

b. How thick a shield is required to reduce the radiation by 99%?

6. (15 points) Determine if  $w$  is a discrete exponential function or a linear function of  $x$ . Explain! Your answer must show that you have used all the values given in the table below.

$x$	-2	-1	0	1	2	3
$w$		75	60	48	38.4	30.72

- a. Write the formula for  $w$  as a function of  $x$  and fill in the value  $w(-2)$ .
- b. Write  $w_x$  in terms of  $w_{x-1}$ .
7. (15 points) A demand curve is given by the equation  $75p + 50q = 300$ , where  $p$  is the selling price in dollars,  $q$  is the quantity demanded at that price. Determine the intercepts of this graph, sketch the graph, and give the real world meaning of the intercepts.