## Math576 Combinatorial Game Theory <br> Homework 1

due midnight of Friday, Sept. 4, 2020
Submission method: Your answers to Homework 1 must be converted into a single pdf file. Then login to Blackboard. Click on assignments/homework1. Upload your answers. You can try to upload twice. Only last version will be graded.

1. Draw two red-blue Hackenbush games with the same game value $\frac{5}{8}$.
2. State the simplicity rule. Use it to find the following game values:
(a) $\left\{\frac{3}{4} \left\lvert\, 2 \frac{1}{4}\right.\right\}$
(b) $\left\{-2,-1 \left\lvert\,-\frac{1}{2}\right.\right\}$
(c) $\left\{0 \left\lvert\, \frac{3}{4}\right., 1\right\}$
(d) $\left\{0,1 \left\lvert\, 1 \frac{1}{2}\right., 2\right\}$
3. Find the values of the following Hackenbush games.

4. Find the value of the following ski-jump game.

| L |  |  |  |
| :--- | :--- | :--- | :--- |
|  | R |  |  |
|  |  |  | L |

5. Find the value of the following Toad-and-Frog game. If Bight Left starts first, what is his best first move? (Left moves Toads (T) eastwards and Right moves Frogs (F) westwards.)

| T |  | F |  |
| :---: | :---: | :---: | :---: |
|  | F | T |  |
| F |  |  | T |

