## Math 777 Homework 2 Due: Feb. 9, before lecture.

- 1. Determine the crossing numbers of the Petersen graph.
- 2. Let  $M_{2n}$  be the graph obtained from the even cycle  $C_n$  by adding chords joining vertices that are opposite. Determine the crossing number  $\nu(M_{2n})$ .
- 3. Decompose  $K_9$  into three pairwise-isomorphic planar graphs.
- 4. Let G be a matching of size n. Select a set of k vertices at a random. Compute the expected number of edges induced by the selected vertices.
- 5. Prove that some 2-coloring of the edges of  $K_{m,n}$  has at least  $\binom{m}{r}\binom{n}{s}2^{1-rs}$  monochromatic copies of  $K_{r,s}$ .
- 6. By examining common neighbors, prove that if p > 0 is fixed and  $o(n/\log n)$ , then almost every G(n, p) is k-connected.