

Use the paper provided. Each problem is worth 10 points.

NO CALCULATORS!

If you e-mail me requesting that I send you your grade, I will do it. Or, get your grade from VIP or TIPS.

1. Compute $\int_0^1 \int_{\tan^{-1} y}^{\frac{\pi}{4}} \sec^5 x dx dy$.
2. Compute $\int_0^1 \int_x^1 e^{-y^2} dy dx$.
3. Compute $\iint_D \left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 dx dy$, where D is the region inside $\left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 = 1$.
4. Find the volume of the solid below $x^2 + y^2 + z^2 = 1$ and above $z = \sqrt{x^2 + y^2}$.
5. Compute $\iint_D (x+y)^3 e^{x-y} dx dy$, where D is the region bounded by $x+y = 1$, $x+y = 5$, $x-y = -1$, and $x-y = 2$.
6. Compute $\iint_D e^{x^2+y^2} dx dy$, where D is the region inside $x^2 + y^2 = 1$.
7. Compute $\iint_S x dS$, where S is the triangle with vertices $(1, 1, 0)$, $(0, 3, 0)$, and $(0, 0, 1)$.
8. Let $\vec{F}(x, y, z) = (e^x \sin y) \vec{i} + (e^x \cos y) \vec{j} + z^2 \vec{k}$. Evaluate $\int_{\vec{c}} \vec{F} \cdot d\vec{s}$, where $\vec{c}(t) = (\sqrt{t}, t^3, e^{\sqrt{t}})$, for $0 \leq t \leq 1$.
9. Evaluate $\iint_S (\nabla \times \vec{F}) \cdot d\vec{S}$ where S is the surface $x^2 + y^2 + 3z^2 = 1$, $z \leq 0$, and $\vec{F} = y \vec{i} - x \vec{j} + zx^3y^2 \vec{k}$.
10. Find $\int_{\mathbf{c}} (3y + x) dx + (8x - 15y) dy$, where \mathbf{c} is the path that starts at $(1, 0)$; travels along the x -axis to $(2, 0)$; travels in the upper half plane along the circle with center $(0, 0)$ and radius 2 to $(-2, 0)$; travels along the x -axis to $(-1, 0)$; and travels in the upper half plane along the circle with center $(0, 0)$ and radius 1 back to $(1, 0)$.