

36 (82)

3. Find  $\int \frac{1}{\sqrt{16 - 9x^2}} dx = \frac{1}{4} \int \sqrt{\frac{dx}{1 - (\frac{3x}{4})^2}} = \frac{4}{3} \frac{1}{4} \int \frac{dy}{\sqrt{1-y^2}} = \frac{1}{3} \sin^{-1} u + C$

$u = \frac{3x}{4}$   
 $du = \frac{3}{4} dx$

$= \frac{1}{3} \sin^{-1} \left( \frac{3x}{4} \right) + C$

4. Let  $f(x) = e^x - x$ . Where is  $f(x)$  increasing, decreasing, concave up, and concave down. Find the local maxima, local minima, and points of inflection of  $y = f(x)$ . Graph  $y = f(x)$ .

$$f'(x) = e^x - 1$$

$$f''(x) = e^x$$

$$f'(x) = 0 \text{ when } x=0$$

$f''(x)$  is always positive

$$\begin{array}{c} f' \text{ neg} \quad | \quad f' \text{ pos} \\ \hline 0 \end{array}$$

$$f'' \text{ pos}$$

- $f$  is incr. for  $x > 0$
- $f$  is dec for  $x < 0$
- $f$  is c-u. for all  $x$
- $f$  is never c.g

loc. min at  $(0, 1)$

no loc. max

no p.o.s

