

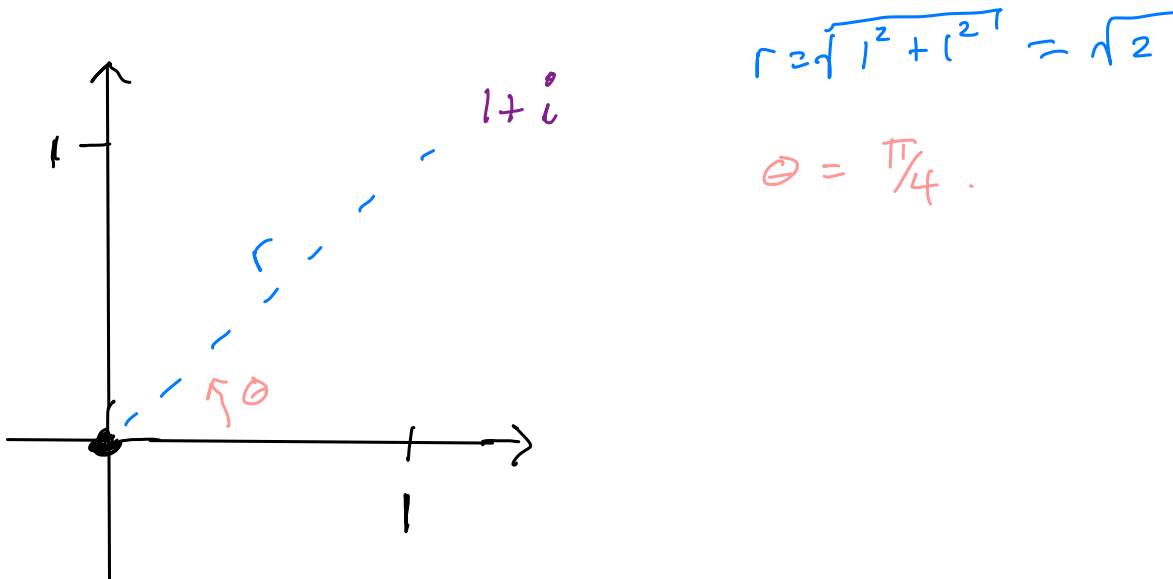
You are **strongly** encouraged to work in groups, following the procedure as in homework [MS09](#).

**Exercise pCA 1.** Express the given complex number in the form  $a + ib$  with  $a, b \in \mathbb{R}$ .

**ER 1.a.**  $(1 + i)^{20}$ . Hint. Express  $(1 + i)$  as  $re^{i\theta}$ .

**ER 1.b.**  $\frac{1 - 2i}{2 + i}$ . Hint. Multiply the numerator and denominator by the *complex conjugate* of  $2 + i$ , which is  $2 - i$ .

(a) Note  $1 + i = 1 + 1i$  so we view  $1 + i \in \mathbb{C}$  as the point  $(1, 1) \in \mathbb{R}^2$ .



So

$$1 + i = \sqrt{2}e^{i\pi/4} \stackrel{\text{note}}{=} \sqrt{2}[\cos(\pi/4) + i\sin(\pi/4)] .$$

So

$$(1 + i)^{20} = (\sqrt{2}e^{i\pi/4})^{20} = (\sqrt{2})^{20}e^{i5\pi} = 2^{10}e^{i\pi} = \boxed{-2^{10}} \text{ or } \boxed{-1024} .$$

(b) Multiplying the numerator and denominator by  $2 - i$ , the complex conjugate of  $2 + i$ , we get

$$\frac{1 - 2i}{2 + i} \cdot \frac{2 - i}{2 - i} = \frac{2 - 2 + (-4 - 1)i}{2^2 + 1^2} = \frac{0 - 5i}{5} = \boxed{-i} .$$