

You are **strongly** encouraged to work in groups, following the procedure as in homework MS09.

Below is a summary of the handout: [Stone-Weierstrasse Theorems](#).

*Recall 1.* About the metric space  $(C(K, \mathbb{K}), d_\infty)$ .

**Theorem 2** (Weierstrass Approx. Thm.). *The collection of real polynomial is dense in  $C([0, 1])$ .*

**Definition 3.** separates points (of  $S$ ) and algebra (of functions over  $\mathbb{K}$ ).

**Theorem 4** (Stone-Weierstrass theorem, real version so  $\mathbb{K} = \mathbb{R}$ ).

**Theorem 5** (Stone-Weierstrass theorem, complex version so  $\mathbb{K} = \mathbb{C}$ ).

**Lemma 6.** *Uniform approximation of the square root function on the unit interval by polynomial.*

### Metric Space Exercise 11.

Do the following Stone-Weierstrass Exercises from the handout [Stone-Weierstrasse Theorems](#).

The [LaTeX](#) file of this handout might save your time.

**MS 11a.** Do SW 4.

**MS 11b.** Do SW 5.