

Exercise.

Let $f, g \in H(G)$, with G is open and connected, satisfy

$$f(z)g(z) = 0 \quad \text{for each } z \in G .$$

Show that $f(z) = 0$ for each $z \in G$ or $g(z) = 0$ for each $z \in G$.