Pin: ??? Variant of **3.3.6** C.

Name: ? Sundstrom §3.3 p126–127. Math 300

The symbol for the rational numbers is  $\mathbb{Q}$  while the symbol for the irrational numbers is  $\mathbb{R} \setminus \mathbb{Q}$ .

So you can express that x is an irrational number by  $x \notin \mathbb{Q}$  or by  $x \in \mathbb{R} \setminus \mathbb{Q}$ .

Recall for any sets R and Q, the set R set minus Q is the set  $R \setminus Q \stackrel{\text{def.}}{=} \{x \in R : x \notin Q\}$ .

Note the difference in direction in the backslash for set minus  $(R \setminus Q)$  and quotient of numbers (1/2 = 0.5).

A symbol for the positive real numbers is  $\mathbb{R}^{>0}$  where  $\mathbb{R}^{>0} = \{x \in \mathbb{R} : x > 0\}$ .

You may use the fact we showed in class that if p is a prime then  $\sqrt{p}$  is irrational.

- **Conjecture C.** For every pair of real numbers x and y, if x + y is irrational, then x is irrational and y is irrational.
- 1. Symbolically write Conjecture C.
- 2. State whether Conjecture C is true or false.
- 3. If Conjecture C is true, then provide a proof of Conjecture C. If Conjecture C is false, then provide a counterexample that shows (and clearly explains why) Conjecture C if false.

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DELETE this whole sentence and THEN put your answer to ALL parts down here.

230108 Page 1 of 1