Pin: ??? Variant of **3.3.6 B**.

Name: ? Sundstrom §3.3 p126–127. Math 300

The symbol for the rational numbers is \mathbb{Q} while the symbol for the irrational numbers is $\mathbb{R} \setminus \mathbb{Q}$.

So you can express that x is an irrational number by $x \notin \mathbb{Q}$ or by $x \in \mathbb{R} \setminus \mathbb{Q}$.

Recall for any sets R and Q, the set R set minus Q is the set $R \setminus Q \stackrel{\text{def.}}{=} \{x \in R : x \notin Q\}$.

Note the difference in direction in the backslash for set minus $(R \setminus Q)$ and quotient of numbers (1/2 = 0.5).

A symbol for the positive real numbers is $\mathbb{R}^{>0}$ where $\mathbb{R}^{>0} = \{x \in \mathbb{R} : x > 0\}$.

You may use the fact we showed in class that if p is a prime then \sqrt{p} is irrational.

- **Example 2.** Conjecture B. For each positive real number x, if x is irrational then \sqrt{x} is irrational.
- 1. Symbolically write Conjecture B.
- 2. State whether Conjecture B is true or false.
- 3. If Conjecture B is true, then provide a proof of Conjecture B. If Conjecture B is false, then provide a counterexample that shows (and clearly explains why) Conjecture B if false.

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DELETE this whole sentence and THEN put your answer to ALL parts down here.

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