

Pin: ???  
Name: ?

The symbol for the rational numbers is  $\mathbb{Q}$  while the symbol for the irrational numbers is  $\mathbb{R} \setminus \mathbb{Q}$ .  
So you can express that  $x$  is an irrational number by  $x \notin \mathbb{Q}$  or by  $x \in \mathbb{R} \setminus \mathbb{Q}$ .  
Recall for any sets  $R$  and  $Q$ , the set  $R$  set minus  $Q$  is the set  $R \setminus Q$   $\stackrel{\text{def.}}{=} \{x \in R: x \notin Q\}$ .  
Note the difference in direction in the backslash for set minus ( $R \setminus Q$ ) and quotient of numbers ( $1/2 = 0.5$ ).  
A symbol for the positive real numbers is  $\mathbb{R}^{>0}$  where  $\mathbb{R}^{>0} = \{x \in \mathbb{R}: x > 0\}$ .  
You may use the fact we showed in class that if  $p$  is a prime then  $\sqrt{p}$  is irrational.

- . **Conjecture A.** For each positive real number  $x$ , if  $x$  is irrational, then  $x^2$  is irrational.
1. Symbolically write Conjecture A.
  2. State whether Conjecture A is true or false.
  3. If Conjecture A is true, then provide a proof of Conjecture A. If Conjecture A is false, then provide a counterexample that shows (and clearly explains why) Conjecture A if false.

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DELETE this whole sentence and THEN put your answer to ALL parts down here.