

# Redo. See Hint.

▷. **Definition.** Let A point  $(x_0, y_0) \in \mathbb{R}^2$  is:

- inside the circle whose equation is  $(x - h)^2 + (y - k)^2 = r^2$  provided  $(x_0 - h)^2 + (y_0 - k)^2 < r^2$
- on the circle whose equation is  $(x - h)^2 + (y - k)^2 = r^2$  provided  $(x_0 - h)^2 + (y_0 - k)^2 = r^2$ .
- outside the circle  $(x - h)^2 + (y - k)^2 = r^2$  provided  $(x_0 - h)^2 + (y_0 - k)^2 > r^2$ .

►. **Theorem 1.** Each point on or inside the circle whose equation is

$$(x - 1)^2 + (y - 2)^2 = 4$$

is also inside the circle whose equation is

$$x^2 + y^2 = 26 .$$

1. Let  $x, h, r$  be real numbers and  $r > 0$ . For each of the following statements, indicate whether the statement is TRUE or FALSE. No justification needed.

- (a) If  $(x + h)^2 \leq r^2$ , then  $|x + h| \leq r$ .
- (b) If  $(x + h)^2 \leq r^2$ , then  $x + h \leq r$ .
- (c) If  $(x + h)^2 \leq r^2$ , then  $-r \leq x + h \leq r$ .
- (d) If  $-3 \leq x \leq 2$ , then  $0 \leq x^2 \leq 4$ .
- (e) If  $-3 \leq x \leq 2$ , then  $0 \leq x^2 \leq 9$ .

2. Symbolically write Theorem 1. Your answer should be of the form, for appropriately chosen inequalities which are the open sentences  $P(x, y)$  and  $Q(x, y)$  ( $\forall (x, y) \in \mathbb{R}^2$ ) [ $P(x, y) \implies Q(x, y)$ ].

3. Prove Theorem 1 algebraically (using (in)equalities), similar to [this linked class example](#). Do **not** use calculus. Do not argue geometrically but rather use geometric idea to form your Thinking Land.

►. **Hint.** If  $(x-1)^2 + (y-2)^2 \leq 4$ , then  $(x-1)^2 \leq 4$  since  $(x-1)^2 = (x-1)^2 + 0 \leq (x-1)^2 + (y-2)^2 \leq 4$ .

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DELETE this whole sentence and THEN put your answer to ALL parts down here.