

▷. **Definition.** Let A point $(x_0, y_0) \in \mathbb{R}^2$ is:

- inside the circle whose equation is $(x - h)^2 + (y - k)^2 = r^2$ provided $(x_0 - h)^2 + (y_0 - k)^2 < r^2$
- on the circle whose equation is $(x - h)^2 + (y - k)^2 = r^2$ provided $(x_0 - h)^2 + (y_0 - k)^2 = r^2$.
- outside the circle $(x - h)^2 + (y - k)^2 = r^2$ provided $(x_0 - h)^2 + (y_0 - k)^2 > r^2$.

►. **Theorem 1.** Each point on or inside the circle whose equation is

$$(x - 1)^2 + (y - 2)^2 = 4$$

is also inside the circle whose equation is

$$x^2 + y^2 = 26 .$$

1. Let x, h, r be real numbers and $r > 0$. For each of the following statements, indicate whether the statement is TRUE or FALSE. No justification needed.

- (a) If $(x + h)^2 \leq r^2$, then $|x + h| \leq r$.
- (b) If $(x + h)^2 \leq r^2$, then $x + h \leq r$.
- (c) If $(x + h)^2 \leq r^2$, then $-r \leq x + h \leq r$.
- (d) If $-3 \leq x \leq 2$, then $0 \leq x^2 \leq 4$.
- (e) If $-3 \leq x \leq 2$, then $0 \leq x^2 \leq 9$.

2. Symbolically write Theorem 1. Your answer should be of the form, for appropriately chosen inequalities which are the open sentences $P(x, y)$ and $Q(x, y)$ ($\forall (x, y) \in \mathbb{R}^2$) [$P(x, y) \implies Q(x, y)$].

3. Prove Theorem 1 algebraically (using (in)equalities), similar to [this linked class example](#). Do **not** use calculus. Do not argue geometrically but rather use geometric idea to form your Thinking Land.

.....

DELETE this whole sentence and THEN put your answer to ALL parts down here.