Pin: ???	Variant of 2.2.13 .
Name: ?	Sundstrom §2.2 p52. Math 300
Important Exercise	Explorations and Activities
Let's compare the below Theorem A and Theorem B. Theorem A . Let x and y be integers.	
If $x \cdot y$ is even, then x is even or	μ is even. (A)
Theorem B. Let x and y be integers.	
If x is odd and y is odd, then $x \cdot$	$y ext{ is odd.} ext{(B)}$
Notice that statement in (A) is of the <u>basic</u> $\langle unquantified \rangle$ sym	polic form of
$P \implies (Q \lor R)$	(0)
where P is " $x \cdot y$ is even", Q is "x is even", and R is "y is even", Write the contrapositive of the conditional statement in (0)	en" (with the understanding $x, y \in \mathbb{Z}$).

- 1. Write the <u>contrapositive</u> of the conditional statement in (0) in basic (unquantified) symbolic form. (Just write the contrapositive of the statement in (0). Do not use DeMorgan (yet). Your solution should have the atoms (i.e.: P, Q, R) joined by logical operators/connectives (so look similar to (0)). Your solution should <u>not</u> have: x, y, English words.)
- 2. Using one of De Morgan's Laws, write a logically equivalent statement to your statement in part 1 in basic $\langle unquantified \rangle$ symbolic form. $\langle Your solution should have the atoms (i.e.: P, Q, R) joined by logical$ operators/connectives (so should look similar to (0)). Your solution should not have: <math>x, y, English words. \rangle
- 3. Using the result from the previous parts of this problem, explain why the statement in (A) is logically equivalent to the statement in (B).

Important lesson learned from this problem.

We just showed (A) and (B) are logically equivalent statements. So to prove (A), we can either prove (A) (as it is written) or prove the logically equivalent (B) (which is the previously shown (in §1.2) result Lemma POO).

Proof of Thm. A. We will proof Theorem A by contrapositive (and DeMorgan). Let x and y be integers. Thus we need to show that if x and y are odd integers then xy is an odd integer.

Let x and y be odd integers. Since x and y are odd integers, by Lemma POO, xy is an odd integer. We have just shown that if x and y are odd integers then xy is an odd integer, which is the contrapositive of Theorem A. Thus Theorem A is true.

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DELETE this whole sentence and THEN put your answer to ALL parts down here.